## RESEARCH PRESESSION

(Final Program)

The 73rd Annual Meeting of the National Council of Teachers of Mathematics

Tuesday-Thursday, 4-6 April 1995

Sheraton Hotel and Towers Boston, MA

Sponsored by

Research Advisory Committee of the National Council of Teachers of Mathematics

Special Interest Group for Research in Mathematics Education of the American Educational Research Association

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#### Announcements

A registration fee of \$5.00 is requested to help defray expenses.

The Tuesday evening session and all Wednesday sessions will be held in the Sheraton Hotel. Consult the final NCTM Program for locations of the Thursday sessions.

Informal meetings may be held Wednesday afternoon in Beacon H.

To preserve the interactive nature of the presession, we remind each organizer/moderator to allow a minimum of 15 minutes per session for general discussion.

## Acknowledgment

Sincere gratitude to Cathryn Speckman for her invaluable help in the preparation of this program.

#### Tuesday, 04 April 1995

7:30 - 9:00 p.m.

Republic B (Sheraton)

#### Welcome

Organizers:

Susan Jo Russell, TERC

Chair, NCTM Research Advisory Committee

George W. Bright, UNC - Greensboro Co-Chair. SIG/RME of AREA

#### The NCTM Standards Six Years Later: Where Are We With Mathematics Education Reform? (Opening Plenary Address)

Moderator:

Mary Lindquist, Columbus College

Panel:

Joan Ferrini-Mundy, University of New Hampshire

Susan Jo Russell, TERC

William Tate, University of Wisconsin Zalman Usiskan, University of Chicago Glenda Lappan, Michigan State University

The panel will highlight issues about the progress of mathematics education reform in three areas: school change, curriculum reform, and equity. Within each area, the panelists will attempt to point to surprises — outcomes of the reform efforts that we may not have expected or to which we may not be paying enough attention. Following the panelists' opening remarks, the audience will consider these issues in small groups. Then the whole group will reconvene for an interaction between audience and panelists.

A reception will be held in Republic A (Sheraton) following this session.

## Wednesday, 05 April 1995

(See center of program for Wednesday's Schedule)

8:30 - 12:00 noon

Beacon B (Sheraton)

## Developing Theory of Mathematics Teaching

Chair: **Deborah Loewenberg Ball.** Michigan State University

Presenters: Martin Simon, Pennsylvania State University

> Megan Franke, University of California at Los Angeles Deborah Schifter, Educational Development Center

Les Steffe, University of Georgia

Jan de Lange. Freudenthal Institute of the Netherlands

This session will explore the need for and recent contributions to theory of mathematics teaching. Representing significant research programs, the panel members will launch a cutting-edge conversation that will include all those present.

8:30 - 12:00 noon

Beacon C (Sheraton)

## Early Development of Algebraic Reasoning

Organizer/Presider: James Kaput, University of Massachusetts-Dartmouth

Jack Smith, Michigan State University Presenters:

Patrick Thompson, San Diego State University Virginia Bastable, Mount Holyoke College

Henri Picciotto. University of California at Berkeley

Jere Confrey, Cornell University
Gail Burrill, University of Wisconsin at Madison

The symposium will address the research, development and policy implications of this enriched, widened and deepened sense of school algebra.

8:30 - 10:00 am

Beacon A (Sheraton)

#### Creating Effective Designs for Using Telecommunications in Inservice Mathematics Education

Organizer/Presenter. Margaret Honey, Education Development Center

for Children and Technology, New York, NY

Marvin Cohen, Bank Street College Presenters:

Barbara Dubitsky, Bank Street College Bob Spielvogel, Center for Children and

Technology

This session will discuss design and development issues involved in the effective use of on-line networks as a tool for professional development in the teaching of mathematics.

8:30 - 10:00 am

Beacon D (Sheraton)

#### Mathematics as a Verb and Not a Noun

Organizer/Presenter: Dr. Claudia Giamati, Northern Arizona University

Dr. Marion Wieland, Greyhills High School Presenters: Ms. Mary Francis Begay, Greyhills High School

The research delves into the differences that have been discovered in the way Navajo students perceive certain mathematical relationships. Its findings present certain ramifications on the teaching, learning and assessment of mathematical knowledge.

8:30 - 10:00 am

Beacon E (Sheraton)

#### The Relevance of Authority to Conceptualizing Reform in Mathematics Education

Organizer/Presenter: Melvin R. (Skip) Wilson, University of Michigan

Presenters: Thomas J. Cooney, University of Georgia

Barry Shealy, State University of New York at Buffalo Betty Hopkins, Edmonson Middle School Lori Brinkerhoff, Edmonson Middle School Michael Goldenberg, University of Michigan

Discussant: Paul Ernest, University of Exeter

Where should and does the authority to determine mathematical correctness lie? Presentations will present varying perspectives on the role of pedagogical authority in mathematics education reform. Teacher educators, researchers, and classroom teachers will discuss theoretical and practical implications of this issue.

8:30 - 10:00 am

Beacon F (Sheraton)

#### Evaluating Curriculum Development Efforts: Models, Issues, and Findings from Three NSF-Funded Projects

Organizer/Presenter. Diana V. Lambdin, Indiana University

Presenters: Glenda Lappan, Michigan State University

Mary Berle-Carman, TERC

Jan Mokros, TERC

Harold Schoen, University of Iowa

Christian Hirsch, Western Michigan University

Discussant: Norman Webb, University of Wisconsin at Madison

Principal investigators and evaluators from three NSF-funded multi-year curriculum development projects (one elementary, one middle-school, and one secondary) discuss issues faced and insights gained through conducting research for the purpose of project evaluation.

## Mathematical Autobiographies: The Impact of Teachers' Early Experiences on Current Perceptions and Decisions

Organizer/Presider: Patricia A. Brosnan, The Ohio State University

Presenters: Jeffrey Smith, The Ohio State University

Diana Erchick, The Ohio State University Gale Watson, West Liberty State College Gayle Millsaps, The Ohio State University

Discussant: Suzanne Damarin, The Ohio State University

Studies of K-12 teachers and preservice elementary teachers showed that early mathematics experiences perpetuated their disposition towards mathematics. Presenters will reveal how teachers' reflections on these early experiences have influenced their current practices and philosophies of teaching and learning.

#### 10:30 - 12:00 noon

Beacon A (Sheraton)

#### Large Scale Professional Development for Teachers of Elementary School Mathematics: Research and Evaluation Issues

Organizer/Presenter: Susan N. Friel, University of North Carolina

Mathematics and Science Education Network

Presenters: George Bright, University of North Carolina at

Greensboro

William Bush, University of Kentucky Rebecca Corwin, TERC

Report from NSF funded conference (11/94) that explored research-based knowledge related to professional development of teachers of elementary school mathematics. An overview of conference and resulting recommendations made to NSF will be provided. Open discussion of research and evaluation issues raised by recommendations will follow.

## 10:30 - 12:00 noon

Beacon D (Sheraton)

## Exploring the Territory before Proof

Presider/Discussant: Dan Chazan, Michigan State University

Organizer/Presenter: Laurie Edwards, University of California at Santa Cruz

Presenters: Carolyn Maher, Rutgers University

Gershon Harel, Purdue University

The session will highlight research which examines the nature of proof and the processes of learning, discovery and communication which occur prior to and apart from conventional, formal proof. The focus will be on students' own forms of argumentation and explanation, with work drawn from studies involving elementary, middle school and university-level students.

## How are the NCTM Standards Documents Being Adapted in Classrooms?: Emerging Issues from Reform-Related Research

Chair: Frank K. Lester, Jr., Indiana University

Organizer/Presenter: Paola Sztajn, Indiana University/CNPq-Brazilian

Government

Joan Ferrini-Mundy, University of New Hampshire Discussants:

Sandra K. Wilcox, Michigan State University

Participants will analyze cases of elementary teachers, looking for social and ideological factors that shape the ways these teachers interpret and implement the Standards. The discussants will provide their visions of reform, and a debate will follow.

#### 10:30 - 12:00 noon

10:30 - 12:00 noon

Beacon F (Sheraton)

#### Multiple Perspectives on Assessment: The Relationship between Theory and Practice

Presider/Discussant: Max Stephens, Victorian Ministry of Education

Organizer/Presenter: David Clarke, University of Melbourne

Susanne Lajoie, McGill University Presenters:

Alan Schoenfeld, University of California

at Berkelev

Martin van Reeuwijk, Freudenthal Institute,

University of Utrecht

Discussant:

Henk van der Kooij, Freudenthal Institute, University of Utrecht

The terms "Authentic Assessment", "Realistic Assessment", "Constructive Assessment" and "Balanced Assessment" can be identified with particular theoretical positions. Advocates of each position will explain and justify the theory underlying their perspective on assessment and use practical examples to illustrate the consequent approach.

## 10:30 - 12:00 noon

Beacon G (Sheraton)

## Solving Ethical Dilemmas

Organizers/Presenter: Judy Sowder, San Diego State University

Presenter: Edward Silver, University of Pittsburgh

We are increasingly encountering ethical dilemmas associated with our research, particularly as we move from quantitative to more qualitative methods. After a brief introduction to moral positions that influence decisions, participants will discuss hypothetical but realistic dilemmas they might encounter.

## Summary of Wednesday Sessions

30-10:00 10:30-noon acon A		1:15-2:45	3:15-4:45			
Honey, Cohen, Dubitsky,	Friel, Bright, Bush, Corwin	Fleener, Ross Pourdavood,	Bradley, Cozzens, Kepner,			
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Creating Effective Designs for	Large Scale Professional	Learning Organizations in	National Science Foundation			
Using Telecommunications in Inservice Mathematics Education	Development for Teachers of	a Quantum Age	Trends and Directions			
Beacon B	Elementary School Mathematics	2				
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Beacon C						
Kaput, Jack Smith, Thompson, Basta	ble, Picciotto, Confrey, Burrill	Monk, Nemirovsky, Noble, Schliemann, Tierney, Wright				
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Beacon D			0			
Giamati, Weiland, Begay	Chazan, Edwards, Maher, Harel	Clements, Sarama, Battista De Villiers	Whitman, Nohda, Hoffer, Lai, Isoda, Li			
Mathematics as a Verb and	Exploring the Territory	Unique Contributions of	Using the van Hiele Theory and the			
Not a Noun	before Proof	Computers to Learning and	NCTM Standards to Compare the			
Beacon E		Teaching Geometry	Geometry			
Wilson, Cooney, Shealy, Hopkins,	Laster Catala D. 1136					
Brinkerhoff, Goldenberg, Ernest	Lester, Sztajn, Ferrini-Mundy, Wilcox	Webb, Kilpatrick, McLeod, Heck, Tate, Hancock, Mewborn, Schappelle, Millissinos, Stake	Silver, Stein, Grover, Henningsen, Graham, Williams			
The Relevance of Authority to	How are the NCTM Standards	Critical Components of Reform	Studying Instructional Practice in a			
Conceptualizing Reform in	Documents being Adapted in	Efforts in Mathematics Education	National Reform Mathematics Project			
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Mokros, Schoen, Hirsch, Webb	Schoenfeld, Reeuwijk,	Samuelson, S. Smith, Souza,	Strutchens, Tate, Cuevas			
Englishing Control D	van der Kooij	Taylor, C. Morrow, J. Morrow				
Evaluating Curriculum Development Efforts	Multiple Perspectives on	Research Related to Gender Issues	Learning from Each Other: Research			
Beacon G	Assessment		Perspectives on Equity in Mathematics			
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Mathematical Autobiographies	Solving Ethical Dilemmas	To Tall on New To Tall I	Shelley, Saenz-Ludlow, Waldamuth			
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Beacon H		That the Question	Two Mathematics Classrooms			
OPEN FOR CONSULTATIONS TI	HROUGHOUT THE DAY	E.				

1:15 - 4:45 p.m.

Beacon B (Sheraton)

Do We Need to Establish Explicit Standards for Research in Mathematics Education?

Moderator:

Thomas J. Cooney, University of Georgia

Presenter:

Frank K. Lester, Jr., Indiana University

Discussants:

Members of the JRME Editorial Panel

This session will consider the value of establishing explicit standards for research in mathematics education. Discussion will be stimulated by a paper prepared by the JRME Editorial Panel on criteria for judging research reports in mathematics education. The paper will be made available to SIG/ RME members prior to the research presession.

1:15 - 4:45 p.m.

Beacon C (Sheraton)

Graphing as a Symbolizing Medium in K-12 Algebra: Teaching and Research Issues

Organizer/Presenter: Stephen Monk, University of Washington

Presenters:

Ricardo Nemirovsky, TERC

Tracy Noble, TERC Analucia Schliemann, Tufts University and TERC

Cornelia Tierney, TERC Tracey Wright, TERC

Graphing, as a symbolizing medium, is central to algebra as a K-12 strand. We will present research documenting students' graphical resources, including their visual, kinesthetic, and narrative senses, and explore with the audience the implications of building mathematical understanding on such personal and expressive capabilities.

T:15 - 2:45 p.m.

Beacon A (Sheraton)

Learning Organizations in a Quantum Age: Are Mathematics Education Research Paradigms Adequate?

Organizer/Presenter: M. Jayne Fleener, University of Oklahoma

Facilitators:

Ross Pourdayood, University of Oklahoma Roland Pourdayood, University of Oklahoma

Habermasian ways of knowing will be related to educational and scientific research approaches. Background information on dissipative structures, chaos theory and open-systems analysis will be offered, then participants will be invited to discuss in small groups mathematics education research paradigms.

T:15 - 2:45 p.m.

Beacon D (Sheraton)

Unique Contributions of Computers to Learning and Teaching Geometry: Multiple Perspectives

Organizer/Presenter.

Douglas H. Clements, State University of New

York at Buffalo

Presenters:

Julie Sarama, State University of New York at Buffalo

Michael T. Battista, Kent State University

Michael DeVilliers, University of Durban -Westville

Are there certain functions computers can perform that other media cannot easily duplicate and that contribute to geometry learning? Researchers using different software environments will lead discussions of the issues involved in the educational application of their software.

1:15 - 2:45 p.m.

Beacon E (Sheraton)

Critical Components of Reform Efforts in Mathematics Education

Organizer/Presenter.

Norman L. Webb, University of Wisconsin at Madison

Jeremy Kilpatrick, University of Georgia Douglas McLeod, San Diego State University Daniel Heck University of Wisconsin at Madison William Tate, University of Wisconsin at Madison Lynn Hancock, University of Georgia

Denise Spangler Mewborn, University of Georgia Bonnie Schappelle, San Diego State University Melissa Mellissinos, San Diego State University

Robert Stake, University of Illinois

The presenters will share findings about critical components of reform in mathematics education from three case studies. Participants will have an opportunity to discuss and react to these findings.

# Research Related to Gender Issues: Theory and Practice

Organizer/Presider: Laura Coffin Koch, University of Minnesota

Presenters:

Judy Gordon, Girls Count, Denver Edie Kort, University of Rochester

Adele Neuberg, Falls Church Schools, Virginia Stan Samuelson, Mount Holyoke College Stephanie Smith, University of Wisconsin at

Madison

Arna Souza, North Kitsap High School

Lyn Taylor, University of Colorado at Denver

Discussants:

Charlene Morrow, Mount Holyoke College Jim Morrow, Mount Holyoke College

This session is designed to involve participants and attendees in a discussion of the theoretical, methodological and practical frameworks related to research in gender issues. The group seeks to interface with other researchers and practitioners who run programs for young women and who are interested in the research questions related to these programs.

1:15 - 2:45 p.m.

Beacon G (Sheraton)

"Reflecting on Practice" Session: To Tell or Not To Tell: Is That the Question?

Organizer:

Research Advisory Committee

Presider/Discussant: Deborah L. Ball, Michigan State University

Presenter:

Patrick Thompson, San Diego State University

Pat Thompson will share a videotape of himself working with a student who had severe difficulty solving problems involving the concept of rate. Despite the current dogma which disdains didactic instruction, the videotape shows him doing a lot of "telling" while working with this student. Participants will analyze this students' thinking and Pat's moves as teacher. The appropriateness - or not - of telling will be a key pedagogical issue in the discussions. Deborah Ball will discuss the substance of the session and the format of "Reflecting on Practice" sessions.

#### National Science Foundation Trends and Directions

Presenter:

3:15 - 4:45 p.m.

John Bradley, National Science Foundation Margaret Cozzens, National Science Foundation Henry Kepner, National Science Foundation Richard Lesh, National Science Foundation Madeleine Long National Science Foundation

Representatives of the National Science Foundation will discuss trends and directions that are likely to take shape over the next few years at the Foundation. There will be an opportunity for members of the audience to ask questions.

7:15 - 4:45 p.m.

Beacon D (Sheraton)

Using the van Hiele Theory and the NCTM Standards to Compare the Geometry Curriculum, Instruction and Students in Japan and Hawaii

Organizer/Presider. Nancy Whitman, University of Hawaii at Manoa

Presenters:

Nobuhiko Nohda, Univ. of Tsukuba Institute of Education

Alan Hoffer, University of California at Irvine

Discussants:

Morris Lai, University of Hawaii at Manoa

Masami Isoda, Univ. of Tsukuba Institute of Education

Yeping Li, University of Pittsburgh

A discussion of cultural differences in the Japanese and Hawaiian geometry curriculum, teaching and student achievement using the NCTM Standards and Japanese Ministry of Education National Courses of Study and the van Hiele theory. The problems of cross-cultural studies will also be discussed.

3:15 - 4:45 p.m.

Beacon E (Sheraton)

Studying Instructional Practice in a National Reform Mathematics Project: Methods and Frameworks used in the QUASAR Project

Presider:

Edward Silver, University of Pittsburgh

Organizer/Presenter. Mary Kay Stein. University of Pittsburgh

Presenters:

Barbara Grover, University of Pittsburgh

Marjorie Henningsen, University of Pittsburgh

Discussants:

**Karen Graham.** University of New Hampshire Steve Williams, Brigham Young University

The methodology and frameworks that have been developed and used to guide the study and interpretation of classroom instruction within the OUASAR Project will be presented and discussed.

3:15 - 4:45 p.m.

Beacon F (Sheraton)

Learning from Each Other: Research Perspectives on Equity in Mathematics Teaching and Learning

Organizers/Panelists: Laurie E. Hart, University of Georgia

Martha Allexsaht-Snider, University of Georgia

Panel Members:

Joanne Rossi Becker, San Jose State University Marilyn Strutchens, University of Kentucky

William F. Tate, University of Wisconsin at Madison

Participants will address the question of how researchers who study gender and those who study issues of race, class, and ethnicity in mathematics education can learn from and serve as catalysts for one another.

3:15 - 4:45 p.m.

Beacon G (Sheraton)

Collaborative Action Research in Two Mathematics Classrooms

Organizer.

Anne M. Raymond, Indiana State University

Presenters:

Brad Hamersley, Honey Creek Middle School
Joanna O. Masingila, Syracuse University
Barbara Shelley, Westhill High School
Adalira Saenz-Ludlow, Purdue University
Cathy Waldamuth, Washington Elementary School

The session is about collaborative action research in mathematics classrooms. Two teams of university researchers and classroom teachers share their collaborative experiences in documenting changes made in each teacher's mathematics classroom. Thursday, 06 April 1995

8:00 - 10:00 a.m.

**TBA** 

Mathematics of Growth and Change: Algebra throughout the Grades (Research Extended Session: Admission by ticket only)

Presenter.

Cornelia Tierney, TERC

This session is #2 in the NCTM program. It was arranged by the Research Presession organizers.

9:00 - 10:00 a.m.

TBA

## Algebra K-12: Prospects and Problems

Presenter:

Stephen Monk, University of Washington

This session is #37 in the NCTM program. It was arranged by the Research Advisory Committee, the Special Interest Group/Research in Mathematics Education, and the National Council of Supervisors of Mathematics.

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