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Accompanying Materials at More4U

Appendix 1

The Big Ideas and Essential Understandings for Addition and Subtraction

Appendix 2

Resources for Teachers

Appendix 3

Tasks

Count, Sort, Compare

How Can You Show ____?

How Many Ways Can They Land?

Macaroni Squeeze Game

Where Are the Guinea Pigs?

Hen and Egg Game

Dot Cards

Corduroy's Pocket, Inside and Out

How Are They Alike?

How Many *Won't Get*?

Translation Task

Sort and Group Basic Facts

Spin, Circle, and Solve

Ring Facts

Livescribe Podcast for “Where Are the Guinea Pigs?” ([link](#))