

# Contents

|   |             |
|---|-------------|
| <b>Preface.....</b>   | <b>vii</b>  |
| <b>Preface to Curriculum Focal Points for Prekindergarten through Grade 8 Mathematics .....</b> | <b>viii</b> |
| <b>Acknowledgments .....</b>  | <b>ix</b>   |
| <b>1. Introduction .....</b>  | <b>1</b>    |
| Purpose of This Guide .....   | 1           |
| Purpose of Curriculum Focal Points.....   | 1           |
| The Impact of Curriculum Focal Points on Curriculum, Instruction, and Assessment .....          | 2           |
| Using This <i>Focus in Grade 8</i> Book.....  | 2           |
| Bringing Focus into the Classroom: Instruction That Builds Understanding and Fluency.....       | 3           |
| An instructional-progression approach .....   | 3           |
| In-depth instructional conversations.....   | 4           |
| Using mathematical representations .....  | 4           |
| An Important Grade 8 Issue: Algebra Readiness .....   | 5           |
| Grade 8 Curriculum Focal Points .....   | 6           |
| <b>2. Focusing on Linear Functions and Linear Equations.....</b>                                | <b>7</b>    |
| Instructional Progression for Linear Functions and Linear Equations .....                       | 7           |
| Early Foundations for Understanding Linear Functions and Linear Equations .....                 | 7           |
| Rational numbers.....   | 8           |
| Proportionality.....  | 9           |
| Equations.....  | 10          |
| Focusing on Linear Functions and Linear Equations .....   | 10          |
| Representations of linear relationships.....  | 10          |
| Slope and $y$ -intercept .....  | 18          |
| Relations and functions.....  | 34          |
| Systems of linear equations.....  | 37          |
| Focusing on Linear Functions and Linear Equations through Problem Solving .....                 | 42          |
| Strengthening Understanding through Connections.....  | 45          |
| Connections in later grades.....  | 47          |
| Developing Depth of Understanding .....   | 48          |

## Contents — Continued

|   |            |
|---|------------|
| <b>3. Focusing on Analyzing Geometric Figures and Space by Using Distance and Angle.....</b>          | <b>49</b>  |
| Instructional Progression for Analyzing Geometric Figures and Space by Using Distance and Angle ..... | 49         |
| Early Foundations for Analyzing Geometric Figures and Space by Using Distance and Angle .....         | 49         |
| Focusing on Analyzing Geometric Figures and Space by Using Distance and Angle .....                   | 52         |
| Inductive and deductive reasoning .....   | 52         |
| Using inductive and deductive reasoning in geometry .....   | 53         |
| Angle relationships in intersecting lines.....  | 54         |
| The sum of the measures of the angles of a triangle .....   | 61         |
| Similar triangles .....   | 63         |
| The Pythagorean theorem and its converse .....  | 67         |
| Focusing on analyzing geometric figures and space through problem solving .....                       | 75         |
| Focusing on Figures and Space through Connections .....   | 80         |
| Connections in later grades.....  | 92         |
| Developing Depth of Understanding .....   | 95         |
| <b>4. Focusing on Analyzing and Summarizing Data Sets .....</b>                                       | <b>97</b>  |
| Instructional Progression for Analyzing and Summarizing Data Sets.....                                | 97         |
| Early Foundations for Analyzing and Summarizing Data Sets .....                                       | 97         |
| Focusing on Analyzing and Summarizing Data Sets.....  | 99         |
| Creating and comparing different data displays.....   | 99         |
| Measures of center.....   | 111        |
| Measures of spread.....   | 121        |
| Scatter plots .....   | 128        |
| Focusing on Analyzing and Summarizing Data Sets through Problem Solving.....                          | 133        |
| Focusing on Analyzing and Summarizing Data Sets through Connections .....                             | 133        |
| Connections in later grades.....  | 137        |
| Developing a Depth of Understanding.....  | 138        |
| <b>5. References.....</b>   | <b>139</b> |