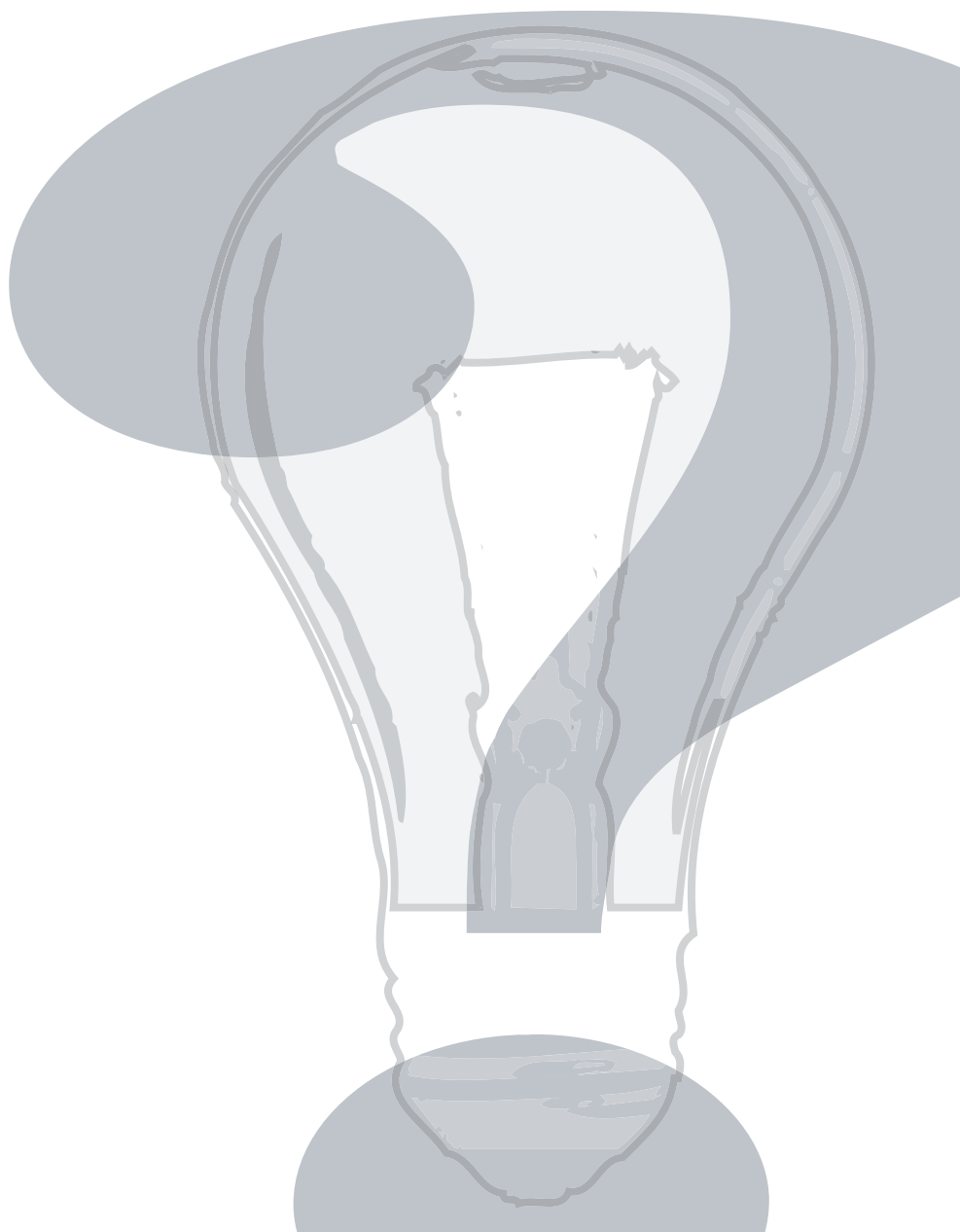


Teaching Mathematics through Problem Solving

Prekindergarten–Grade 6



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