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Accompanying Materials at More4U

Appendix 1

The Big Ideas and Essential Understandings for Geometry and Measurement

Appendix 2

Resources for Teachers

Appendix 3

Tasks