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MTMS, February 1998

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Activities for Junior High School and Middle School Mathematics,
Vol. 2, 1999
TCM, April 1996

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