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## Accompanying Materials at More4U

### Appendix 1

The Big Ideas and Essential Understandings for Statistics

### Appendix 2

Resources for Teachers

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### Appendix 3

#### Tasks

Inventing Activities

Trampoline Testing

Rocket Testing

Developing an Estimator

Raffling to Support Recycling

Raffle Ticket Template