



contents

Volume 109, Number 4, November 2015

features

- 256 Talking Circles Promote Equitable Discourse**
Marcus Hung
 A structured discussion format disrupts patterns of stratified talk and facilitates broader student participation.
- 262 Narrowing Participation Gaps**
Victoria Hand, Karmen Kirtley, and Michael Matassa
 By noticing students' contributions as individuals or part of the team, teachers can focus on engagement.
- 270 HOLA: Hunt for Opportunities-Learn-Act**
Rochelle Gutiérrez
 Suggestions for listening to Latin@ students in their everyday interactions.
- 284 Communities for and with Black Male Students**
Christopher C. Jett, David W. Stinson, and Brian A. Williams
 Four strategies can be effective in creating supportive learning environments.
- 290 Celebrating Diversity by Sharing Multiple Solution Methods**
Woong Lim, Hongjoong Kim, Lynn Stallings, and Ji-Won Son
 A classroom vignette presents teaching practices that develop an appreciation of diverse thinking.
- 298 Assessments That Promote Collaborative Learning**
Maika Watanabe and Laura Evans
 Students practice classroom norms and take responsibility for one another's learning.

on the cover

Classroom communities embrace individuals and foster communication. But how do we, as teachers, make that happen? The feature articles in this Focus Issue highlight ways to capitalize on the diversity in our schools. Equitable discourse, student participation, opportunities to listen, supportive environments, variety, and collaboration—all play a role in establishing strategies and norms that we can adopt or adapt for our own classrooms.

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MATHEMATICS teacher

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departments

- 244 **From the Editorial Panel**
Creating Classroom Communities
- 245 **Reader Reflections**
- 246 **Media Clips**
Generations and Generations//
Mid-Parental Height
Carly Ziniuk
- 252 **Mathematical Lens**
The 100-Block Walk for Math (Part 2)
- 278 **November Calendar and Solutions**
- 306 **Connecting Research to Teaching**
Using Appropriate Tools Strategically
for Instruction
Milan Sherman and Charity Cayton
- 311 **Technology Tips**
Using Graph Theory to Understand
First Nations Connections
Jehu Peters and Don Metz
- 314 **Delving Deeper**
The Inequality of Arithmetic and Geometric
Means from Multiple Perspectives
Richard Askey, Ryota Matsuura, and Sarah Sword
- 319 **For Your Information**
Publications
- 320 **The Back Page: My Favorite Lesson**
Dynamic Right Triangles
*Melike Yiğit Koyunkaya, Signe Kastberg, James
Quinlan, Michael Todd Edwards, and Jane Keiser*

more**4U**

Look online for these additional items:

- Connecting Research to Teaching (p. 306): A GeoGebra file for an activity about intersecting chords

The more4U content, an additional benefit, is for members only.



252 |

calls for manuscripts

- 297 **Call for Chapters: Annual Perspectives in Mathematics Education (APME) 2017**
- 305 **2017 Focus Issue: Nurturing Persistent Problem Solvers**

in the next issue

Coming in December 2015/January 2016:

- "Teaching in a World with PhotoMath," by Corey Webel and Samuel Otten
- "Engaging Students in Survey Design and Data Collection," by Marla A. Sole
- "Reasoning and Sense Making Begins with the Teacher," by Lindsay M. Keazer and Rahul S. Menon