



# contents

Volume 109, Number 5, December 2015/January 2016

## features

- 334 Engaging Students in Survey Design and Data Collection**  
*Marla A. Sole*  
By piloting their own survey on texting while driving, students learn that only unambiguous questions can produce credible results.
- 342 Reasoning and Sense Making Begins with the Teacher**  
*Lindsay M. Keazer and Rahul S. Menon*  
Action research leads a classroom teacher to a new approach and a new role.
- 351 Customizing a Math Course with Your Students**  
*Mark F. Russo*  
A high school math class designed around students' interests and ideas lifts their attitudes toward mathematics and their overall achievement.
- 368 Teaching in a World with PhotoMath**  
*Corey Webel and Samuel Otten*  
As new computation technologies become available, algebra teachers can choose to ban them, limit their use, or use them as an opportunity to reevaluate learning goals.
- 374 Integrating Modeling Steps into the High School Curriculum**  
*Ted Wendt and Kevin Murphy*  
Textbook word problems can be modified to change the way the questions are posed without changing the prerequisite content.

## on the cover

New technology gives teachers and students an opportunity to select tools for a particular task. Learning goals can be more than just getting an answer—we want students to see structure, appreciate strategic approaches, and avoid situations in which they use a tool blindly or indiscriminately. Think about “Teaching in a World with PhotoMath” (pp. 368–73) as authors Corey Webel and Samuel Otten advocate for activities that suit the particular capabilities of human beings.



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## departments

### 324 **Reader Reflections**

### 326 **Media Clips**

Taxes and Percentages: Don't Discount Them!//  
Toilet Paper Producers on a Roll?

*Cara Hubbell and Steve Phelps*

### 330 **Mathematical Lens**

Lessons on Politeness

### 355 **December 2015 and January 2016 Calendars** Calendars and Solutions

### 380 **Activities for Students**

Making Sense of Representations: Card Sorting

*Kate Meredith Raymond*

### 387 **Technology Tips**

Understanding Algebra Graphs Using  
SmartGraphs

*Jessica Ulcickas MacKenzie, Andy Zucker,  
and Carolyn J. Staudt*

### 393 **Delving Deeper**

Summation Formulas Involving Polynomials

*Tom N. Chu*

### 398 **For Your Information**

Publications

### 400 **The Back Page: My Favorite Lesson**

Max the Real Estate Agent

*Diana L. Moss and W. Max Sabo*



330 |

## calls for manuscripts

### 350 **On the Front Burner: Emerging Issues in Mathematics Education**

### 367 **Call for Chapters: Annual Perspectives in Mathematics Education (APME) 2017**

### 373 **Technology Tips**

### 379 **The Back Page: My Favorite Lesson**

### 392 **2017 Focus Issue: Nurturing Persistent Problem Solvers**

more**4U**

Look online for these additional items:

- Reader Reflections (p. 324): A proof of convergence (Tu)
- Activities for Students (p. 380): Tables of values and templates for creating the full-sized cards for two activities
- Delving Deeper (p. 393): Student solutions and templates of the floor plan
- The Back Page (p. 400): Template of floor plan and student solutions

The more4U content, an additional benefit, is for members only.

## in the next issue

Coming in February 2016:

- "Illustrating the Central Limit Theorem," by Mimi Corcoran
- "Speaking Up and Speaking Out about Gender in Mathematics," by Laurie H. Rubel
- "Connecting Functions in Geometry and Algebra," by Scott Steketee and Daniel Scher