What concerns do you hear stakeholders raise about mathematics education today?

We work in the fog of collective amnesia.

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A Brief History of Mathematics Education: Lessons for Today

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Presentation is Posted at NCTM.org/larson

Goals

• Examine a brief (and incomplete) history of school mathematics.

• Demonstrate that the issues we face today are not new, but rather cyclical and seemingly intractable.

• Recommend action steps to break the “intractable” cycle of resistance.

Obstacles to Implementing Research-Informed Instructional Practices

Dominant cultural beliefs about the teaching and learning of mathematics continue to be obstacles to consistent implementation of effective teaching and learning in mathematics classrooms.

The First American School Mathematics Textbook

The first American mathematics textbook was Nicolas Pike’s Arithmetic (1788). The teaching process in Pike’s book was: state a rule, given an example, and have students complete a set of practice exercises.

The Gravitation Pull of History

This approach established a script for mathematics teaching and learning that became deeply embedded in our culture and expected by students and parents alike... consequently nearly every adult has the same idea of what a mathematics teacher is supposed to do.


Teaching is a Cultural Activity

[Teachers]... acquire their training by observing what their teachers do... The methods they use to teach--the ways in which they interact with students around the content--are likely to be determined by their own experiences as students in K-12 classrooms.


The Inertia of the Past is Very Hard to Overcome

Americans live in the shadow, still, of the ideas and stereotypes about arithmetic first articulated in the nineteenth century.


The First Attempt to Understand

The first effort to change the teaching script was Warren Colburn’s An Arithmetic on the Plan of Pestalozzi (1821).


Colburn Introduces “Discovery” Learning to the United States

Colburn’s approach used a series of carefully sequenced questions and concrete materials so students could discover rules for themselves. He argued that problems were to be reasoned out... rather than solved by the direct application of rules... Arguing that teachers postpone practice until after students develop understanding.


Backlash to Colburn was Quick and Eerily Prescient

The Southern and Western Calculator (Bridge 1831) declared that rules were necessary and pupils could not be expected to invent them.

Backlash to Colburn was Quick and Eerily Prescient

The Common School Arithmetic (Botham, 1832) proclaimed that it would satisfy parents who longed for arithmetic to be taught "the good old fashioned way" with concise and plain explanations of rules.

The Great School Mathematics Debate

So within the first half century of the founding of the United States, the great school mathematics debate was established. Should teachers offer students rules and facts to memorize? Or should they give students material to reason about in order to discover and develop understanding of underlying mathematical principles?


The "Intractable" Issues

The two most persistent questions in mathematics education have been and continue to be:

1. What should be the nature of mathematics that students learn – facts, skills, and procedures or concepts and understanding?
2. How should students learn mathematics – teacher directed with a focus on memorization, or student centered through reasoning and discovery?


1930s: William Brownell’s Meaning Theory of Learning

The ultimate purpose of arithmetic instruction is the development of the ability to think in quantitative situations. The work "think" is used advisedly: the ability to merely perform certain operations mechanically and automatically is not enough. Children must be able to analyze real or describe quantitative situations. (p. 28).


1940s-1980s:

Crisis-Reform-Reaction

- WWII: American recruits did not have sufficient basic computational and problem solving skills.
- Soviet launching of Sputnik in 1957.

New Math: 1950s and 1960s

Led by mathematicians, New Math sought to emphasize the underlying structure of mathematics and conceptual understanding rather than the learning of isolated skills and facts ... they wanted students to understand the structure of mathematics, how mathematical ideas fit together, and the reasoning methods of pure mathematics – “habits of mind of mathematicians.”


Notable NSF Funded Projects

• School Mathematics Study Group [SMSG], led by mathematician Edward Begle.
• University of Maryland Mathematics Project [UMMaP]
• University of Illinois Committee on School Mathematics [UICSM]

Backlash to New Math

In an article in the Washington Post, parent James Shackelford described his frustration with his daughter’s new math homework. He complained that as a Ph.D. chemist, he should be able to understand his daughter’s elementary math homework, but couldn’t because it was overly and unnecessarily complicated.


The belief emerged that new math lowered computational skills. This perception became popularized in books like Morris Kline’s Why Johnny Can’t Add.


Research on the effectiveness of new math generally shows only small differences between student achievement in traditional and new math programs.


Reflective Question: Could New Math Have Succeeded?

Proponents of new math could have focused on making sure students ‘understood’ the mechanisms behind the traditional algorithms, thereby making them ‘meaningful.’ Instead, they focused on introducing an entirely new way of conceptualizing arithmetic ...
1970s and 1980s: Back to the Basics

This period emphasized procedural arithmetic skills, clearly defined behavioral objectives, direct instruction aimed at student mastery of the objectives, and the extensive use of local and national standardized tests to measure student attainment of mostly low-level, skill-oriented objectives.


The 1980s: The Origin of Standards-based Reform

- NCTM’s Agenda for Action (1980) – recommended problem solving become the focus of school mathematics and that basic skills should be defined more broadly than simple arithmetic.
- Publication of A Nation at Risk (1983) created an environment that once again made it possible to attempt to reform mathematics education.


Curriculum and Evaluation Standards for School Mathematics, 1989

By the mid-1990s, forty-one states had created state standards or curricular frameworks consistent with the NCTM Standards.


The NCTM Standards

- 1989
- 1991
- 1995
- 2000
- 2006

Backlash to the Standards

By the late 1990s, criticism of the Standards emerges and it was all too familiar: the new standards did not sufficiently emphasize procedural skills, not enough emphasis on direct instruction, not enough practice and memorization, etc.

Backlash to the Standards

The Central Issue:
Parents expected teachers to fulfill the traditional role of transmitter of knowledge to students, but reformers asked teachers to encourage students to do their own thinking.


Early 2000s: Two Major Attempts to Find Peace in the Math Wars

Adding it Up, National Research Council (2001)


National Research Council: Adding it Up

Procedural fluency and conceptual understanding are often seen as competing for attention in school mathematics. But pitting skill against understanding creates a false dichotomy.

National Mathematics Advisory Panel Report

All-encompassing recommendations that instruction should be entirely 'student centered' or 'teacher directed' are not supported by research ... the curriculum must simultaneously develop conceptual understanding, computational fluency, and problem solving skills."


In the Same Decade of Adding it Up and NMAP, We Get NCLB

No Child Left Behind fundamentally changed the focus of instruction. Increasingly between 2002 and the early 2010s, math instruction focused on content to be assessed on state tests -- assessments that tended to assess skills and concepts at a low cognitive-demand level.

NCLB: Unintended Consequences

- States created an incoherent system of 50 different sets of standards, tests, and passing scores.
- Demonstrated overstatements of student learning on state tests compared to NAEP results created fertile ground for the concept of the Common Core to gain traction.


In the Beginning

The political response to the birth of the Common Core was a relatively uncontroversial endeavor and a bipartisan initiative. Both democrat and republican governors supported the standards. Some of the governors who later opposed the standards, originally supported them.


Objections to Standards Today

- Confusion between standards and testing of standards – the “opt-out” movement.
- Confusion between standards and curriculum or instructional strategies.
- Social media – opinion versus evidence.


Where Does the General Public Get Its Information About School?

Evidence indicates that most people in the U.S. get their information about education and schools from family and friends – not from research literature or experts.

Seeing What We Want to See

[Many individuals] seem to find pedagogical burning bushes in the standards that no one else seems to see. Sometimes it seems as if the common core is simply a big, blank projection screen for what people want to see.


These Concerns Aren’t New

When frustration sets in for students, parents, or teachers, there is a tendency to want to place blame. The Common Core (Standards Today) became a bogeyman for every concern anyone had about mathematics education. With respect to most of these concerns, the bogeyman existed prior to 2010, but now he had a new, high-profile identity.


If it Seems We Fight the Same Battles Over and Over Again … It is Only Because We do

The issues in school mathematics are “cyclical and seemingly intractable.”


Breaking the Cycle of Resistance

The issues in school mathematics are “cyclical and seemingly intractable.”

We Have to Answer These Two Historic Questions in Ways that Resonate with Parents

1. What should be the nature of mathematics that students learn – facts, skills, and procedures or concepts and understanding?
2. How should students learn mathematics – teacher directed with a focus on memorization, or student centered through reasoning and discovery?


Recommendations

Moving Forward
We need to start by listening more carefully to all our stakeholders (critics) and understand their hopes and fears for their children and our students – we need to emphasize common ground.

1. Point Out that Much is the Same

- Emphasize that the goal today is not that different from the past: know how (procedural skill), know why (conceptual understanding), and know when (application).
- We are doing nothing more than valuing traditional mathematical learning goals while broadening the definition of mathematical literacy to meet today’s needs.

2. Emphasize that Mathematical Literacy is Multifaceted

How, Why and When while building a Positive Mathematics Identity!

Parents respond best to messages that emphasize critical thinking and problem solving.

3. Emphasize Problem Solving, Strategic Competence and Disposition

Why We Need Multidimensional Mathematics Learning

The product of deeper learning is transferable knowledge, including content knowledge in a domain and knowledge of how, why, and when to apply this knowledge to answer questions and solve problems.

Mathematical Skills are Highly Valuable

The median entry-level salary for college educated STEM majors is the highest of major groups and nearly twice that of high school graduates. In addition, STEM majors experience the largest wage growth over the course of their careers.
### Emotional Connections are Important

Voters tend to resist change even when faced with facts.


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### 4. Help People Separate the Issues

- Standards
- Instruction (curriculum)
- Assessment

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### 5. Show Parents the Strategies!

It is critical not to confuse instructional strategies intended to build understanding with end goals that include proficiency with traditional approaches.

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\begin{array}{c|c|c}
43 \times 17 & 40 + 3 & 21 \\
2 & 10 & 280 \\
17 & 400 & 400 \\
301 & 30 & 731 \\
430 & 731 & 731 \\
\end{array}
\]

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### 6. Advocate for Research-Informed Instructional Practices

Everyone expects physicians to use research-informed and current treatments.


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### Moving Forward: Support and Implement Research-Informed Instructional Practices

The six guiding principles constitute the foundation of high-quality mathematics education.

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### 7. Appropriate and Valid Assessment is Not the Enemy

Assessment diagnoses student learning needs and facilitates effective instruction just as medical tests diagnose illness and direct effective treatment protocols.

Assessment is an Invaluable Tool of High-Quality Instruction

If the country is to make progress on improving mathematics education, then the all-too common aversion to assessment among professional educators ... is untenable. Testing (in some form) is critical to education.


8. Confront the Homework Issue

• It isn’t parents’ responsibility to “do” homework. In fact that can do more harm than good.
• Parents should support perseverance, monitor progress, and ask questions.


9. Provide Evidence this Works

Show parents how and why changes to math instruction help students learn. When this is done support increases.
• Provide evidence that changes improve student learning.


We Have Seen Improved Mathematics Learning

Math achievement in this country is up over the long-term ... Since we've been doing Standards-based reform!


10. We Have to Change the Discourse

Our conversations must move away from misinformation, misguided rhetoric, and extremes – that stuff that grabs headlines and often characterizes tweets and Facebook posts – that do nothing to improve mathematics teaching and learning.

We Must Change the Discourse

Americans have long complained about the quality of mathematics education ... If the discourse ten years from now is to be something other than a refrain about why U.S. mathematics education does not work, a different strategy is needed.

The Call to Action:

We must all take more seriously our role as advocates for high quality math instruction for each and every student. We cannot leave advocacy to others.