

# Moving Achievement Together Holistically: The MATH Project

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Mathematics Education

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<https://bit.ly/3iQtZr6>

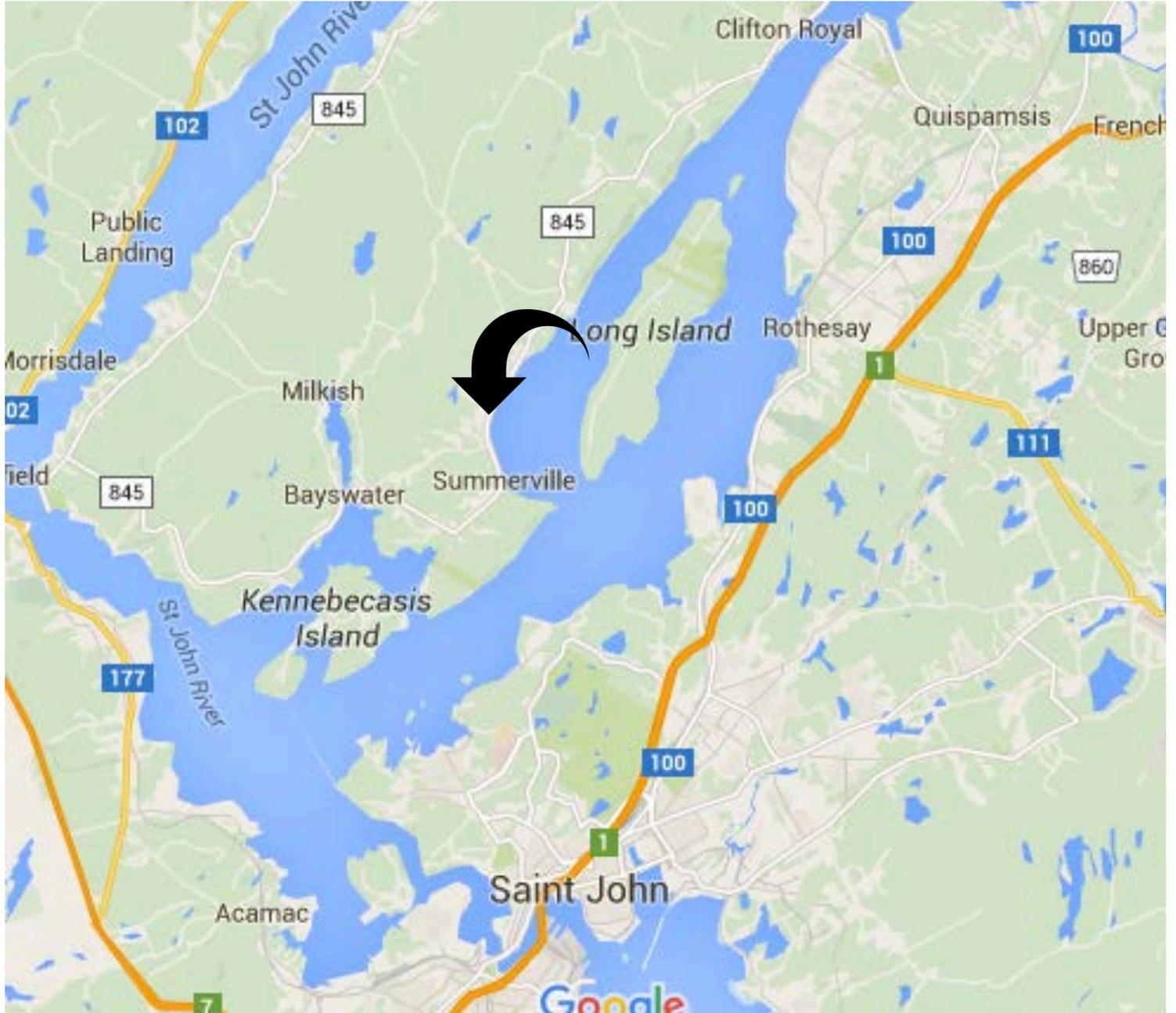


@LLB\_315

# Positioning Myself...

- Wabanaki Confederacy:  
Mi'kmaw, Wulastoyiqik,  
Passemequody, Penobsquis
- Mi'kma'ki – 7 districts that lie  
to the East of the Wulastuk  
river (now known as the St.  
John River)
- Evidence to show the Mi'kmaw  
lived here for over 20,000 years
- Acadians settled in NS in the  
late 1500s and early 1600s
- Black Loyalists arrived in NB  
and NS in the late 1780s;  
having fought alongside the  
British in the war of  
Independence, they were  
granted land and freedom in  
Mi'kma'ki.





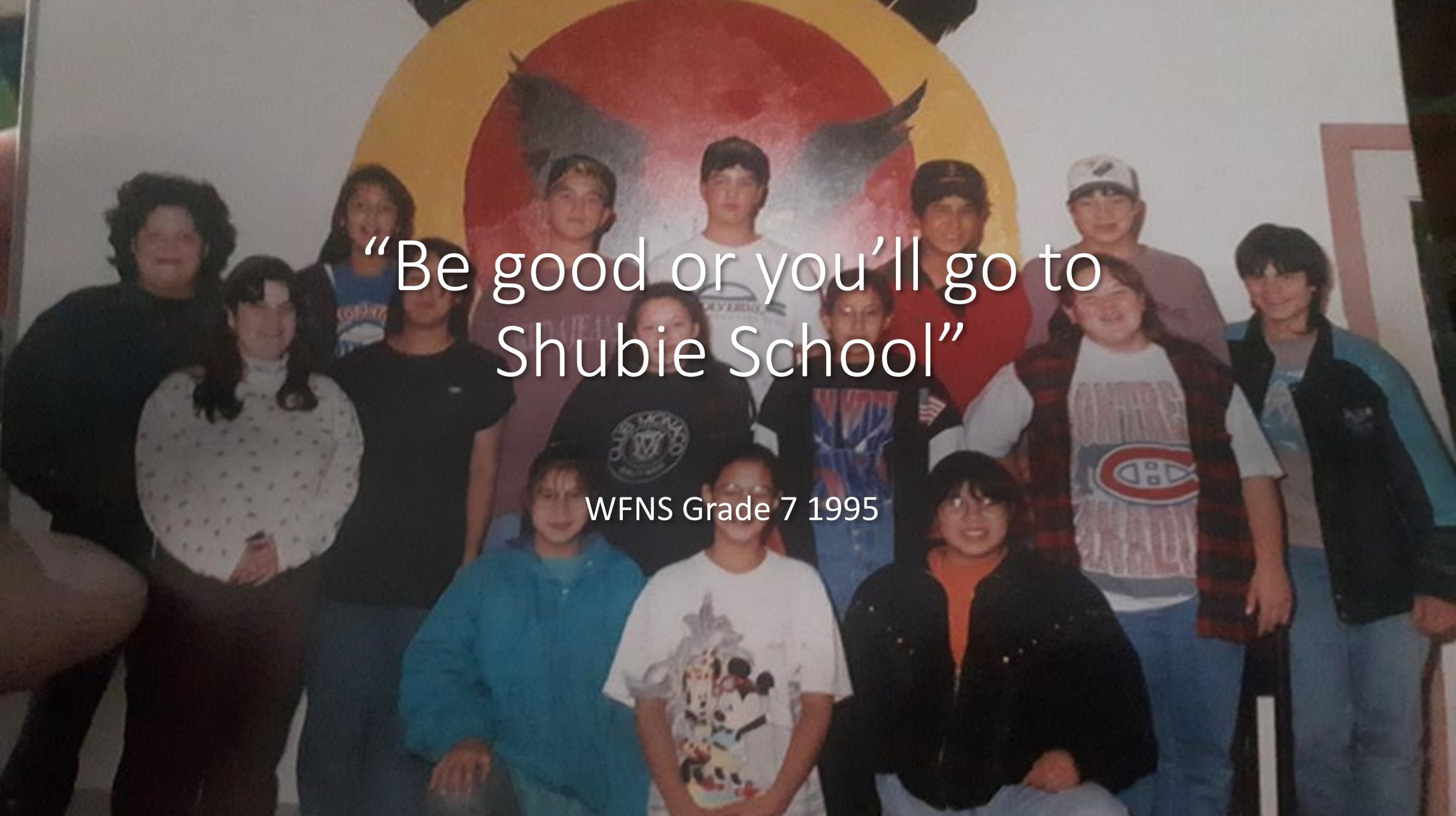


# X-Project

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# Mi'kmaw Kina'matnewey





“Be good or you’ll go to  
Shubie School”

WFNS Grade 7 1995

# How can Math Teachers Address the Call to Action of the TRC? How can we Decolonize?

- Understanding the role of Settler Colonialism on Education, including math education
  - As Tuck and Yang (2012) have stated, "Settler colonialism is different from other forms of colonialism in that settlers come with the intention of making a new home on the land, a homemaking that insists on settler sovereignty over all things in their new domain. [...] In order for the settlers to make a place their home, they must destroy and disappear the Indigenous peoples that live there" (p. 5-6).
  - Cultural genocide is the destruction of those structures and practices that allow the group to continue as a group. States that engage in cultural genocide set out to destroy the political and social institutions of the targeted group. Land is seized, and populations are forcibly transferred and their movement is restricted. Languages are banned. Spiritual leaders are persecuted, spiritual practices are forbidden, and objects of spiritual value are confiscated and destroyed. And, most significantly to the issue at hand, families are disrupted to prevent the transmission of cultural values and identity from one generation to the next. (Truth and Reconciliation Commission, of Canada, 2015, p. 1)
- Recognizing the discourses that reinforce these ideologies
- Unlearning and Relearning

In our  
schools,  
whose math  
are we  
doing?

- “School mathematics curricula emphasizing terms like Pythagorean theorem and pi perpetuate a perception that mathematics was largely developed by the Greeks and other Europeans.” (Gutiérrez, 2017 p. 17)
- Joseph (2010) has argued that ideological beliefs about European superiority meant that “The contributions of the colonized peoples were ignored or devalued as part of the rationale for subjugation and dominance” (p. 4)
- Aikenhead (2017) has referred to this phenomenon as “mathematics myth blindness” (p.121) and pointed out that mathematics’ “privileged status rests on the myth that its Platonist content is acultural, universalist, value free, objective in its use, and nonideological” (p.121).
- Reconciliation and decolonization ask us to address this inequity in mathematics education. We need to tell different stories.



2. a) Write a linear system to model this situation:  
A store sold Inukshuk replicas made with either 6 or 7 stones.  
The total number of stones in all Inukshuit sold was 494. The store sold 13 more Inukshuit made with 6 stones than those made with 7 stones.
- b) Solve this problem: How many of each type of replicas were sold?

9. Talise folded 545 metal lids to make cones for jingle dresses for herself and her younger sister. Her dress had 185 more cones than her sister's dress. How many cones are on each dress?

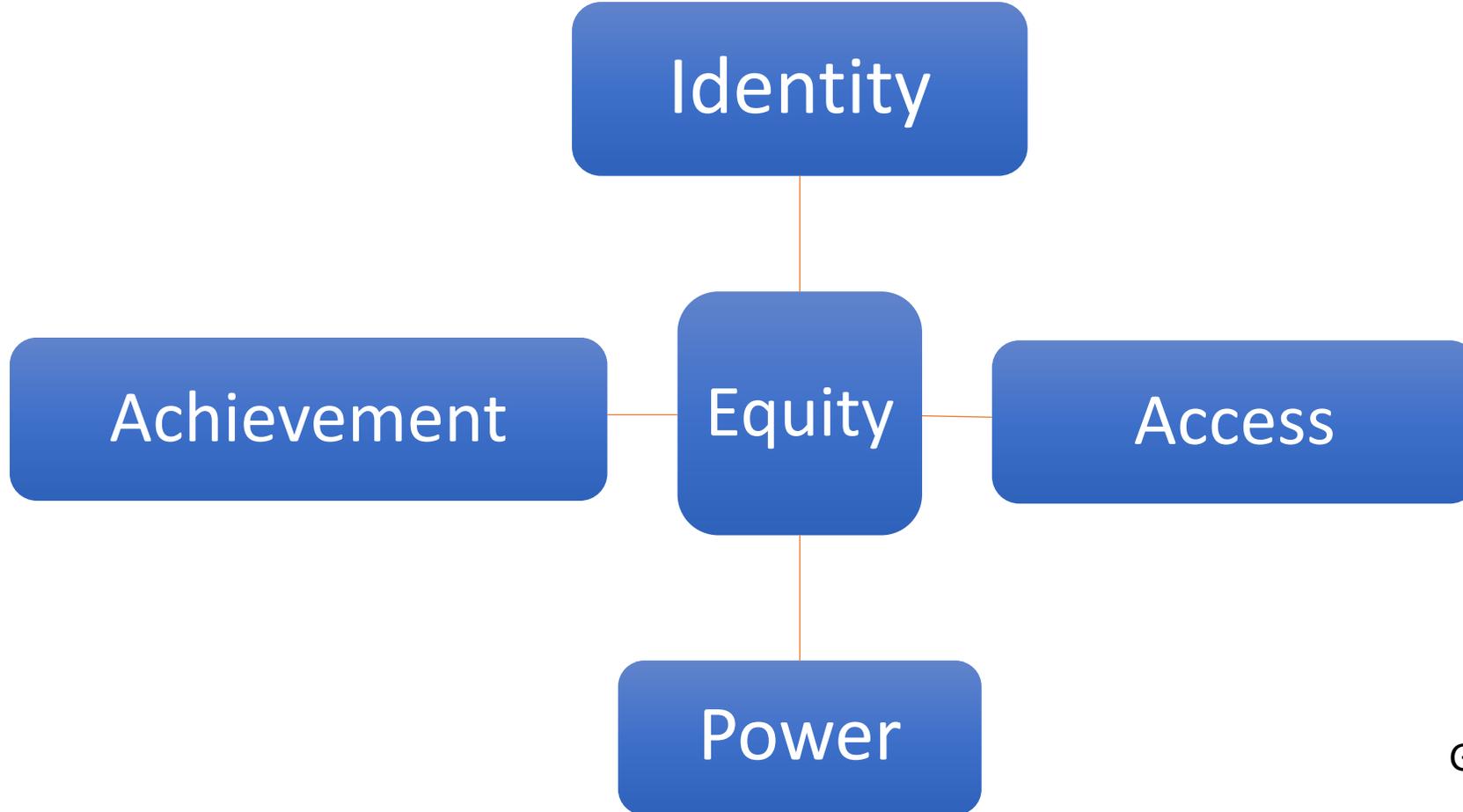


11. Louise purchased a Métis flag whose length was 90 cm longer than its width. The perimeter of the flag was 540 cm. What are the dimensions of the flag?



What textbook companies think reconciliation looks like...They're wrong!

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Gutiérrez (2012)

# Redefining Equity

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## Dianne's Quill Boxes

- The late Dianne Toney was a Mi'kmaw elder who made quill boxes like the one in the picture. She always made them by starting with a circle of bark for the top on which she made her pattern. She would always start at the centre of the circle to make her pattern. After that she would make the ring for the top from strips of wood. To ensure the ring was the right size, Dianne said she would measure three times across and add a thumb. She claimed this would make a perfect ring every time.

- Does this always work?

- <https://teacher.desmos.com/activitybuilder/custom/563159e8adf49b1e06d63c4a>

# Show Me Your Math!



- Began in **2007**
- Inviting Children to be the mathematics researchers
- Where is the math in your community?
- Local Math Fairs
- Annual Regional Math Fair





“I’m the last one who can do this...”

- Picture from:  
<http://www.danielnpaul.com/MargaretGrannyJohnson.html>

Birch bark biting... "I remember Auntie Caroline doing that at the basket shop"



# Maple Syrup Making...

## Sap to Syrup

### Facts:

- A gallon of maple syrup weighs 11 pounds.
- The sugar content of sap averages 2.5% sugar content of maple syrup is at least 66% or more.
- It takes 40 liters of sap to make maple syrup.
- It takes 1 gallon of maple syrup to produce 8 pounds of maple candy or sugar.

### Collecting Sap

Where we tapped the trees- funny fact trail.

What did we use to tap the trees- we used a power drill.

How deep the snow was- At least 45cm.

The first time we went up we took snowshoes to stomp a trail to make it easier to carry up the tubes and buckets. The next time we went up we took the tubes, buckets, power drill and taps. We tapped the trees and waited for the sap to run through the tubes.

Days passed and we waited, we got a little bit of sap the first time. One day it was warm and then night fell and it got cold and we got lots of sap.

### How Far We Went

The distance from the school to trees that we tapped is 1.2 kilometers, but we took 8 days to do that because it is a 7th day.

### How to make maple syrup:

1. Measure the tree
2. Use a power drill of a drill
3. Place the tap into the tree then insert the tube
4. Cut a hole into a bucket big enough to fit the tube into the bucket
5. The only way for the sap to run is if it's warm in the day and cold in the night
6. After it stops doing that tap in the summer all the sap stops running so it's done and day might be in the day warm in the night.

### Temperature Difficulties

Date	Temp	Notes
April 17th	10°C	Good
April 18th	12°C	Good
April 19th	15°C	Good
April 20th	18°C	Good
April 21st	20°C	Good
April 22nd	22°C	Good
April 23rd	25°C	Good
April 24th	28°C	Good
April 25th	30°C	Good
April 26th	32°C	Good
April 27th	35°C	Good
April 28th	38°C	Good
April 29th	40°C	Good
April 30th	42°C	Good

### Thum

Step 1. Measure the tree

Step 2. Use a power drill of a drill

Step 3. Place the tap into the tree then insert the tube

Step 4. Cut a hole into a bucket big enough to fit the tube into the bucket

Step 5. The only way for the sap to run is if it's warm in the day and cold in the night

Step 6. After it stops doing that tap in the summer all the sap stops running so it's done and day might be in the day warm in the night.

### Total Materials We Used

Item	Quantity	Notes
Power Drill	1	Used to tap the trees
Tubes	10	Used to collect sap
Buckets	10	Used to collect sap
Taps	10	Used to tap the trees
Snowshoes	2	Used to stomp a trail
Measuring Tape	1	Used to measure the tree
Power Drill	1	Used to tap the trees
Tubes	10	Used to collect sap
Buckets	10	Used to collect sap
Taps	10	Used to tap the trees
Snowshoes	2	Used to stomp a trail
Measuring Tape	1	Used to measure the tree

## TRY IT YOURSELF

### Drill Your Own Tree!

- Step 1. Drill 3 inches on the side of the tree.
- Step 2. Put the tap in the hole.
- Step 3. Attach tube to the tap.
- Step 4. Put tube in the bucket.
- Step 5. Pour the water (Sap) into the top hole.

Repeat

## Problem's And Solution's

### Problem's

- 1. A major problem was that the weather was not good and it was raining a lot.
- 2. Another problem was that the trees were not healthy and we had to use a power drill to tap them.
- 3. A third problem was that the trees were not healthy and we had to use a power drill to tap them.
- 4. A fourth problem was that the trees were not healthy and we had to use a power drill to tap them.
- 5. A fifth problem was that the trees were not healthy and we had to use a power drill to tap them.
- 6. A sixth problem was that the trees were not healthy and we had to use a power drill to tap them.
- 7. A seventh problem was that the trees were not healthy and we had to use a power drill to tap them.
- 8. An eighth problem was that the trees were not healthy and we had to use a power drill to tap them.
- 9. A ninth problem was that the trees were not healthy and we had to use a power drill to tap them.
- 10. A tenth problem was that the trees were not healthy and we had to use a power drill to tap them.

### Solution's

- 1. We used a power drill to tap the trees.
- 2. We used a power drill to tap the trees.
- 3. We used a power drill to tap the trees.
- 4. We used a power drill to tap the trees.
- 5. We used a power drill to tap the trees.
- 6. We used a power drill to tap the trees.
- 7. We used a power drill to tap the trees.
- 8. We used a power drill to tap the trees.
- 9. We used a power drill to tap the trees.
- 10. We used a power drill to tap the trees.

## GPS



Making a Drum...



Making a Canoe paddle... "It made me feel real Mi'kmaq making my own paddle."

.....

# Wholeness

- Wholeness resists fragmentation, thus quality mathematics experiences require *cultural synthesis* bringing together cultures and values from mathematics and the community, *personal holism* including the child's experiential, conceptual, and spiritual development, and *intergenerational interaction*. (Lunney Borden & Wagner, 2011)



# Reconciliation

- Goal is to “restore what must be restored, repair what must be repaired, and return what must be returned” (Truth and Reconciliation Commission of Canada, 2015, p. 6).



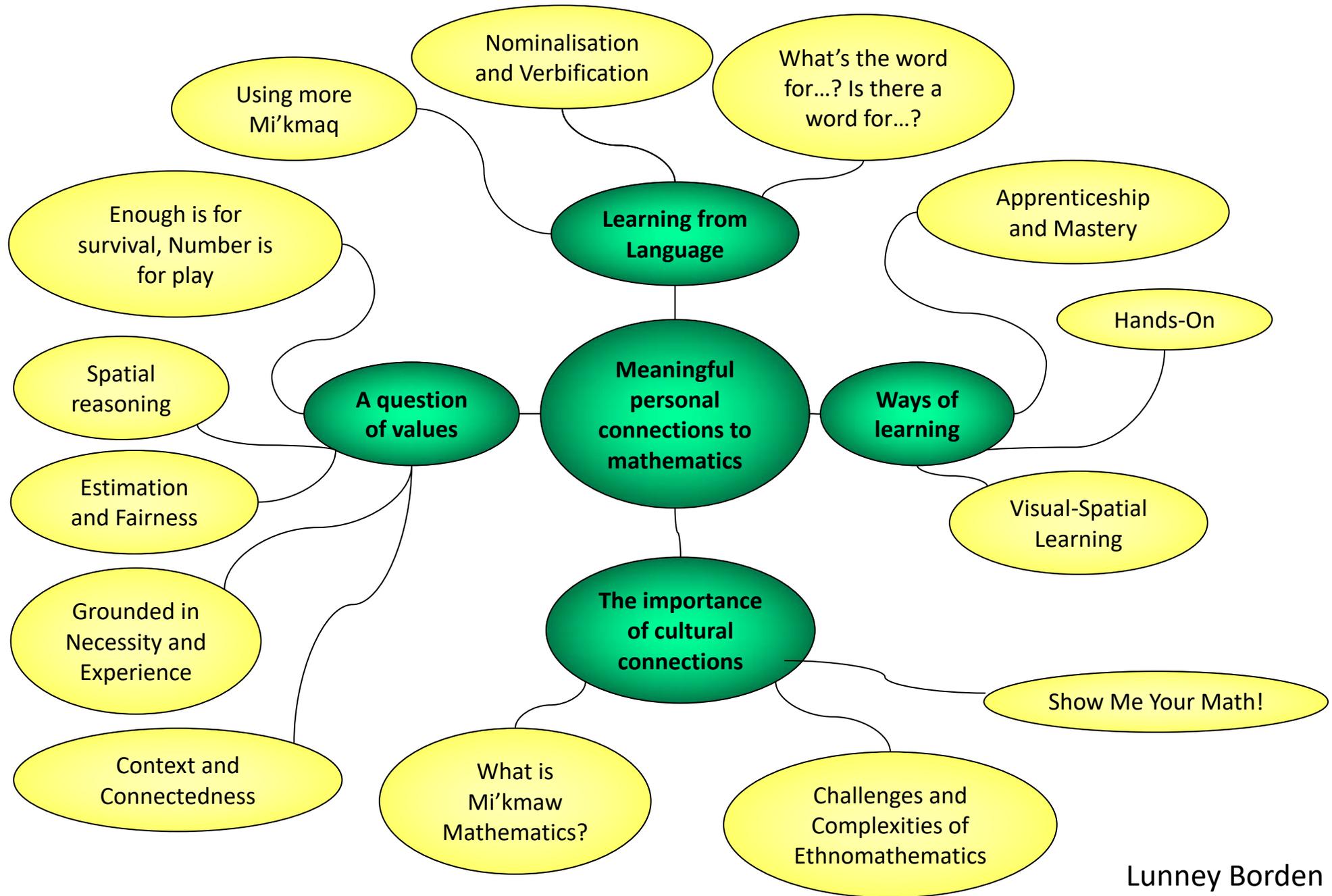
# L'nui'ta'simk

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“Within mathematics education, we have convinced ourselves that “equity” is a strong enough agenda when maybe revolution should be the goal.” Gutiérrez, 2017, p. 11

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Often we believe ethnomathematical investigations alone are enough, but they are not. We must also consider ways in which we can teach math with and through Indigenous ways of knowing, being and doing – L'nui'ta'simk!



# Research Question:

- How can the implementation of the Mawikinutimatimk Framework (Lunney Borden, 2010) for transforming mathematics education in Mi'kmaw communities contribute to increased achievement in these schools across different school contexts serving Mi'kmaw children?
  - How does the professional learning support teacher development? How does the implementation vary across the different contexts?
  - What types of learning and assessment tasks help to improve student learning across these contexts?
  - How do students respond to this approach to learning mathematics in the varying contexts? Does this approach improve engagement and attitude toward learning mathematics?
  - How does the involvement of elders and community knowledge holders in professional learning and classroom teaching support teacher learning and student learning across these contexts?

math is everywhere



math SP5S Jobs

## Our Current Focus

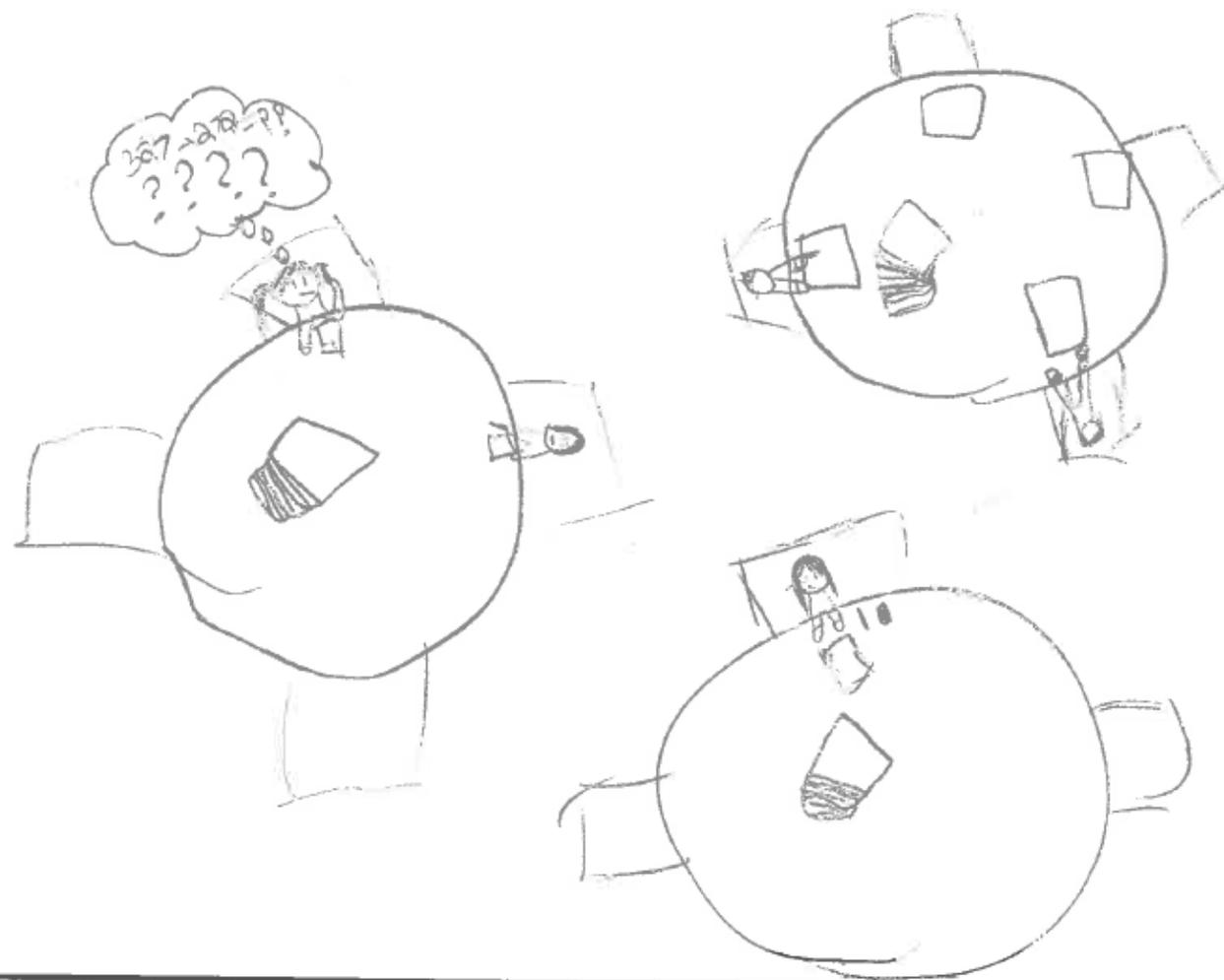
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- Working alongside teachers to help them develop an understanding of the model and consider the implications for teaching and learning
- Verbing and Spatializing Math Teaching and Learning
  - Designing tasks and noticing how students engage with those tasks
- Understanding students perceptions of mathematics
- Working with MK on developing a holistic assessment and learning tasks that support our overall goals (Currently just grade 1)

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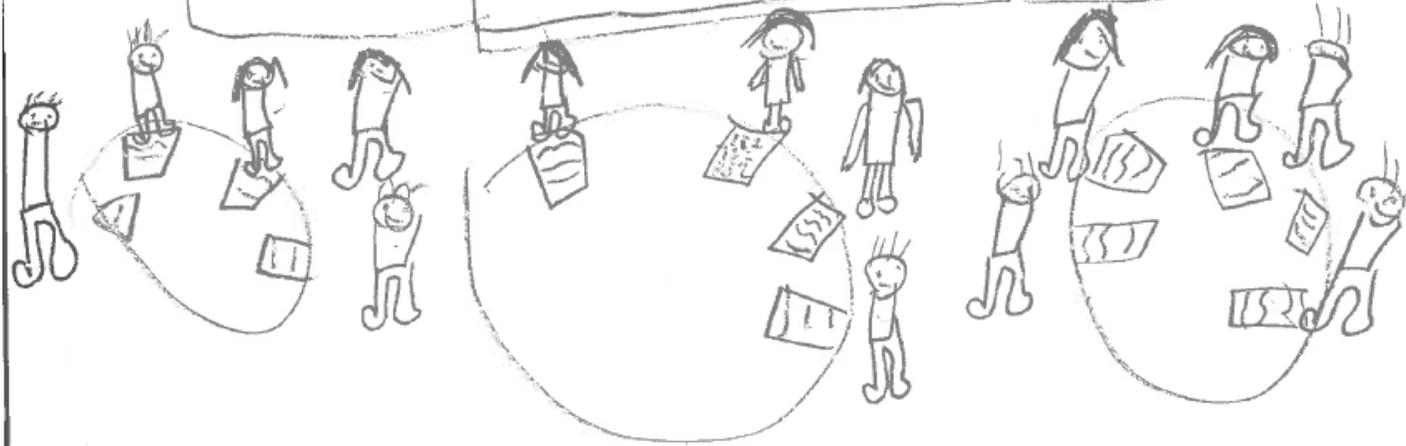
## A Picture of Me Doing Math

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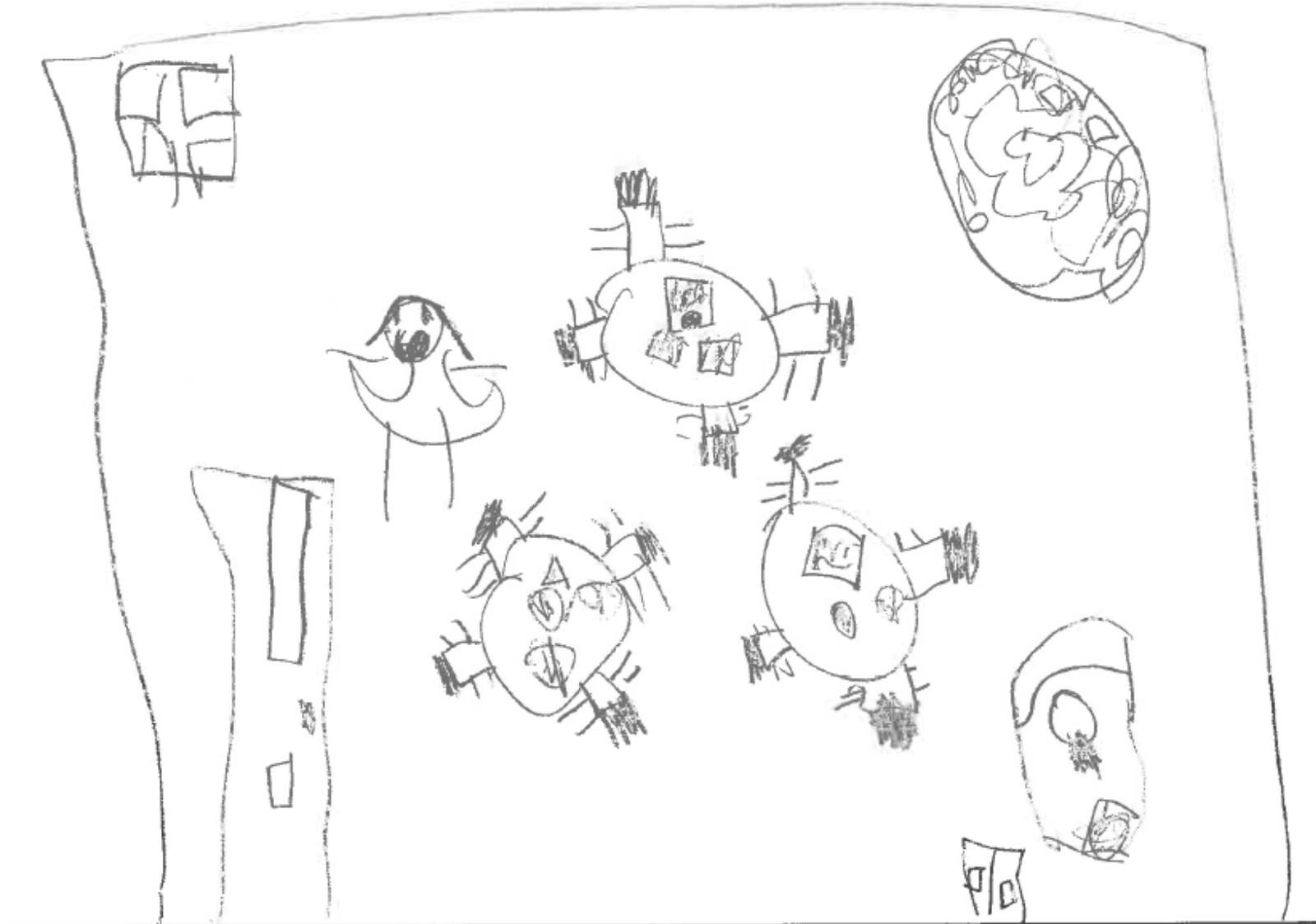


$$162 + 72 = 882$$
$$5192 + 219 = 7384$$

Ellentlisat kylätevan  
= math



Math Class

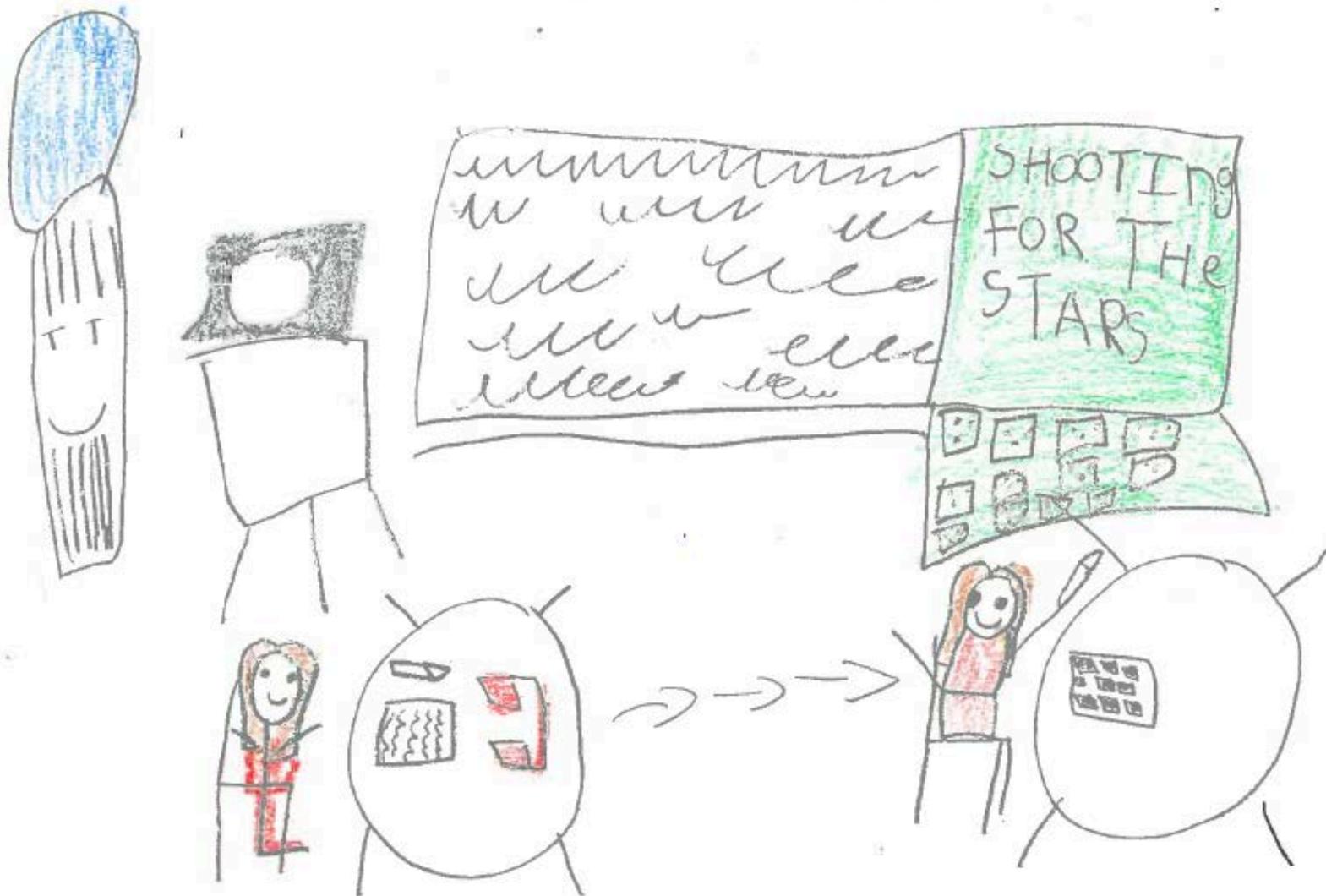


				Math Class					
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Math class  
to pay ok

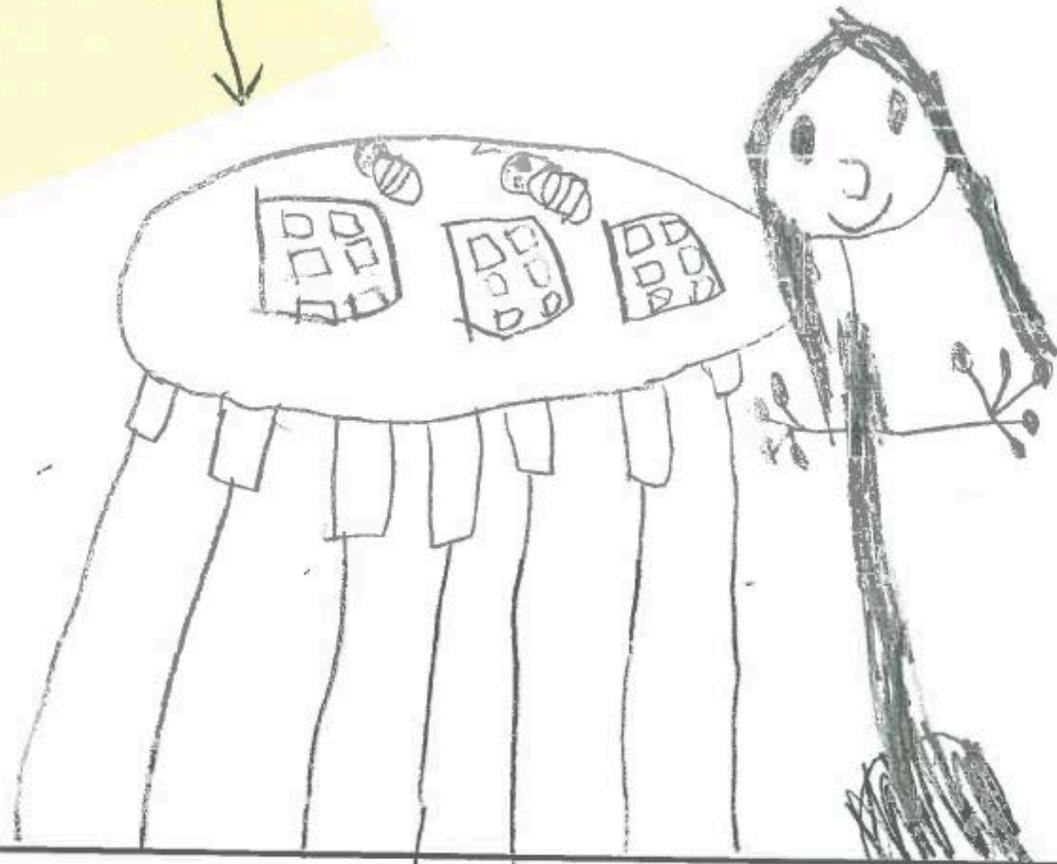
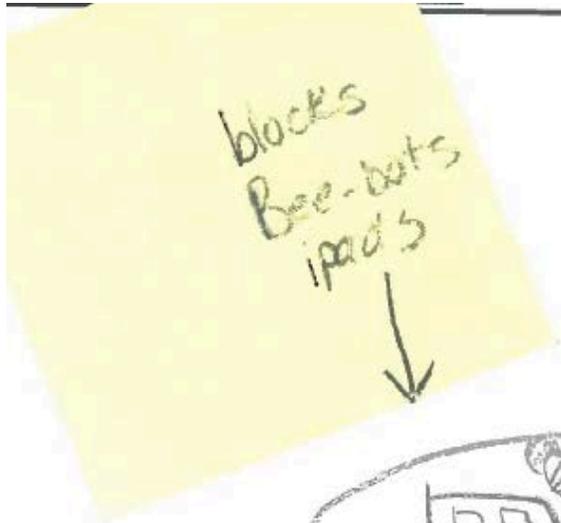


# A PICTURE OF ME DOING MATH



### A Picture of Me Doing Math

blocks  
Bee-bats  
ipad's

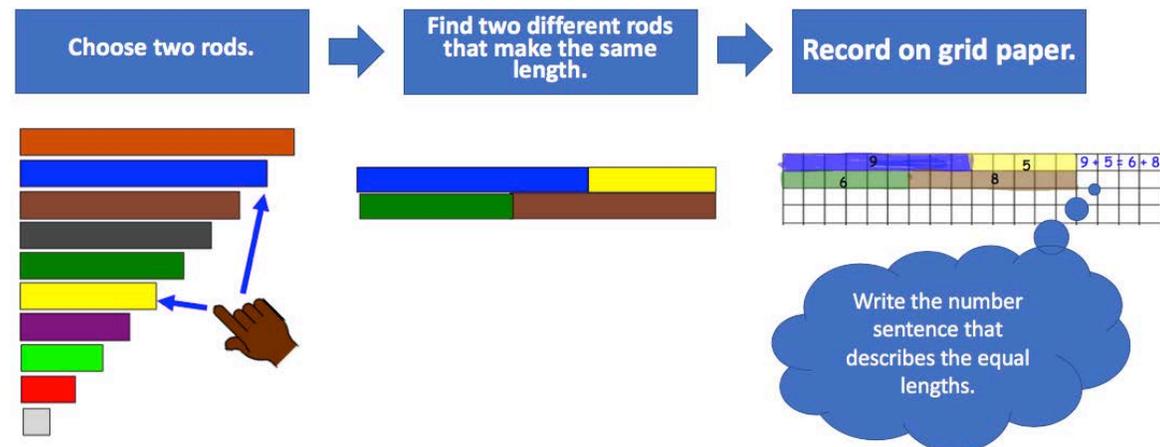
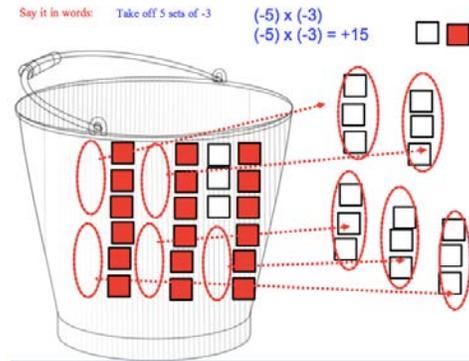


# Findings

- Shared drawings with participating teachers to have them co-analyse with us;
- The emphasis on learning centres
  - Classes were collaborative
  - Children saw math as engaging in multiple modes of learning a concept in centres
  - Teachers believe that centres are the best way to teach as it gives them freedom to work individually or in small groups with students
  - Teachers couldn't imagine any other way of teaching

# Verbing

- Focus on change/motion
- How do I make it?
- What happens if...?
- How is it changing?



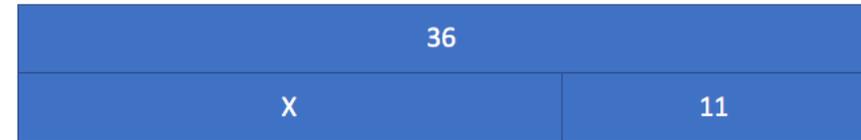
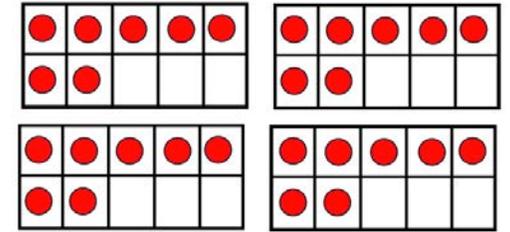
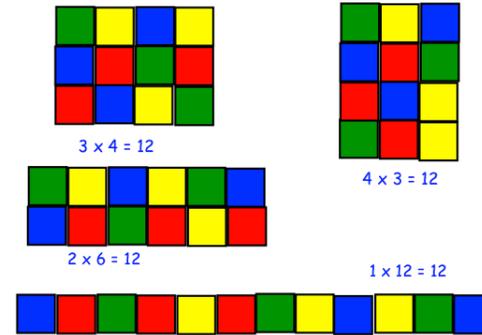
# Spatializing

Linear

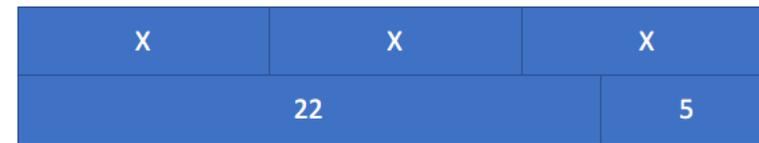
Set

Area

Hold it in your hand



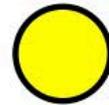
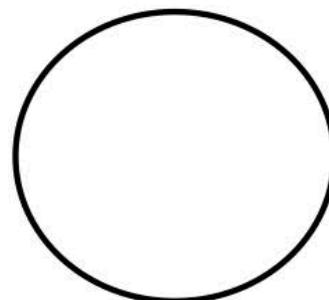
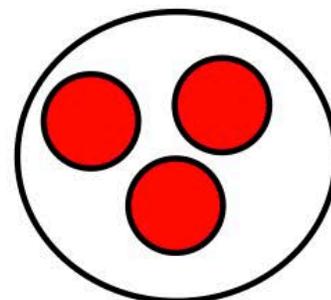
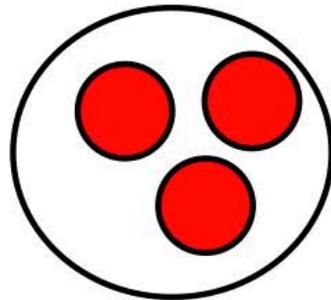
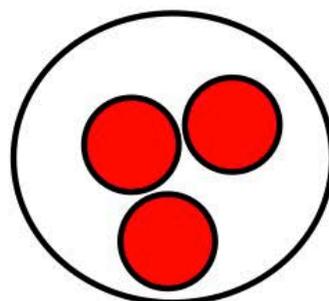
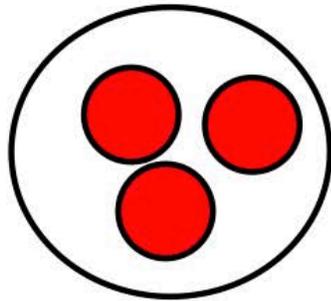
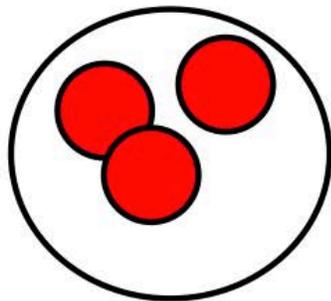
$$X + 11 = 36$$



$$3x - 5 = 22$$

Build 5 sets of 3.

Roll two dice to find the numbers for the blanks.

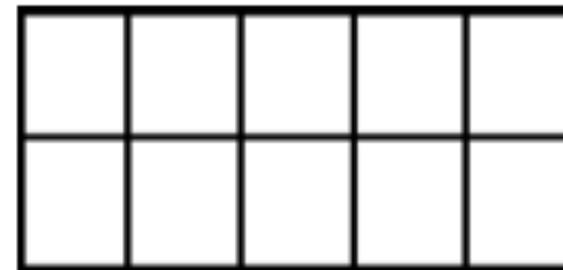
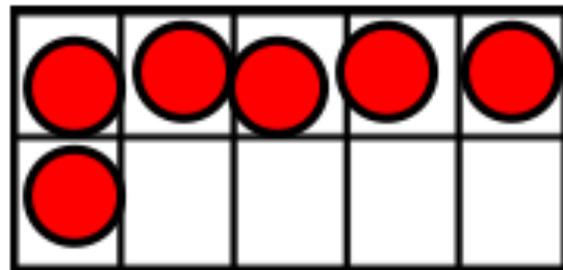
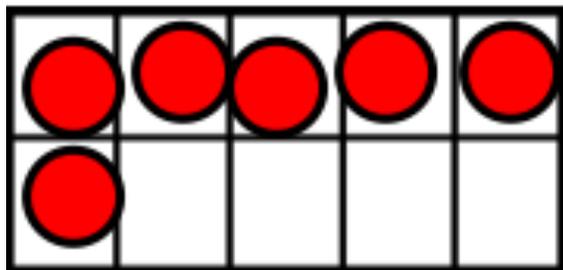
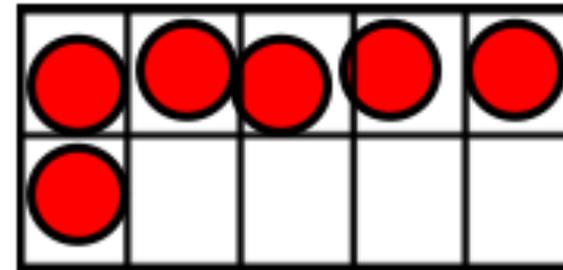
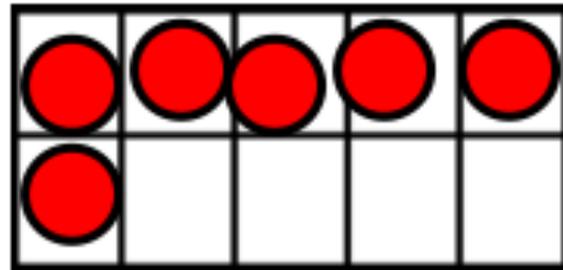
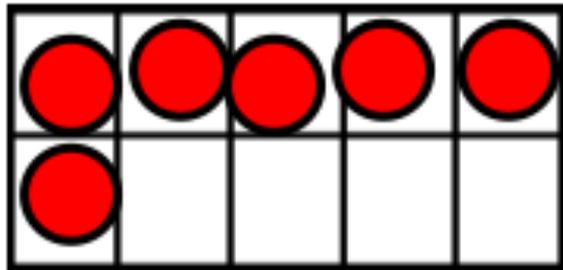


Record your results on the recording sheet.

5 sets of 3 is 15.

Build 5 sets of 6.

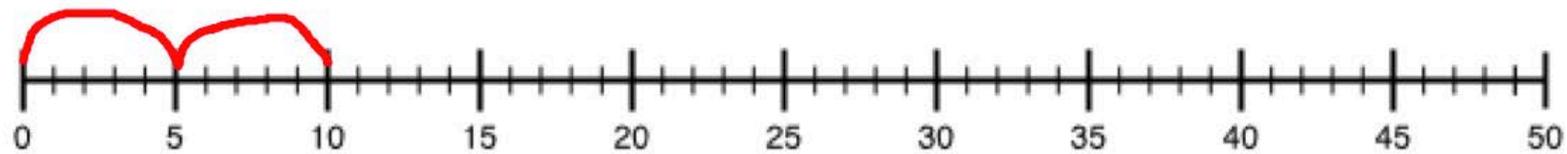
Roll two dice to find the numbers for the blanks.



Record your results on the recording sheet.

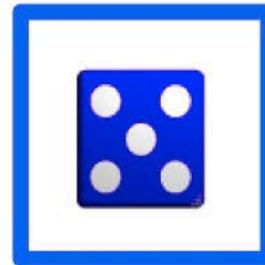
Take 2 jumps of 5.

Roll two dice to find the numbers for the blanks.



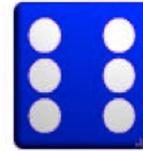
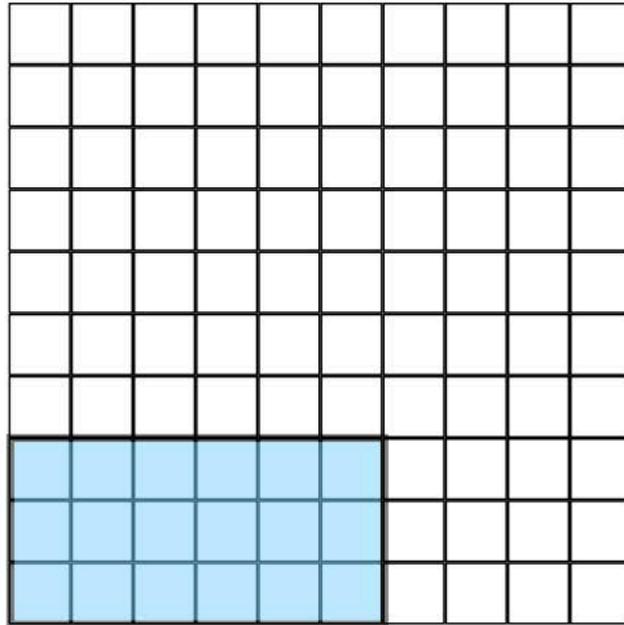
2 jumps of 5 is 10.

Record your results on the recording sheet.



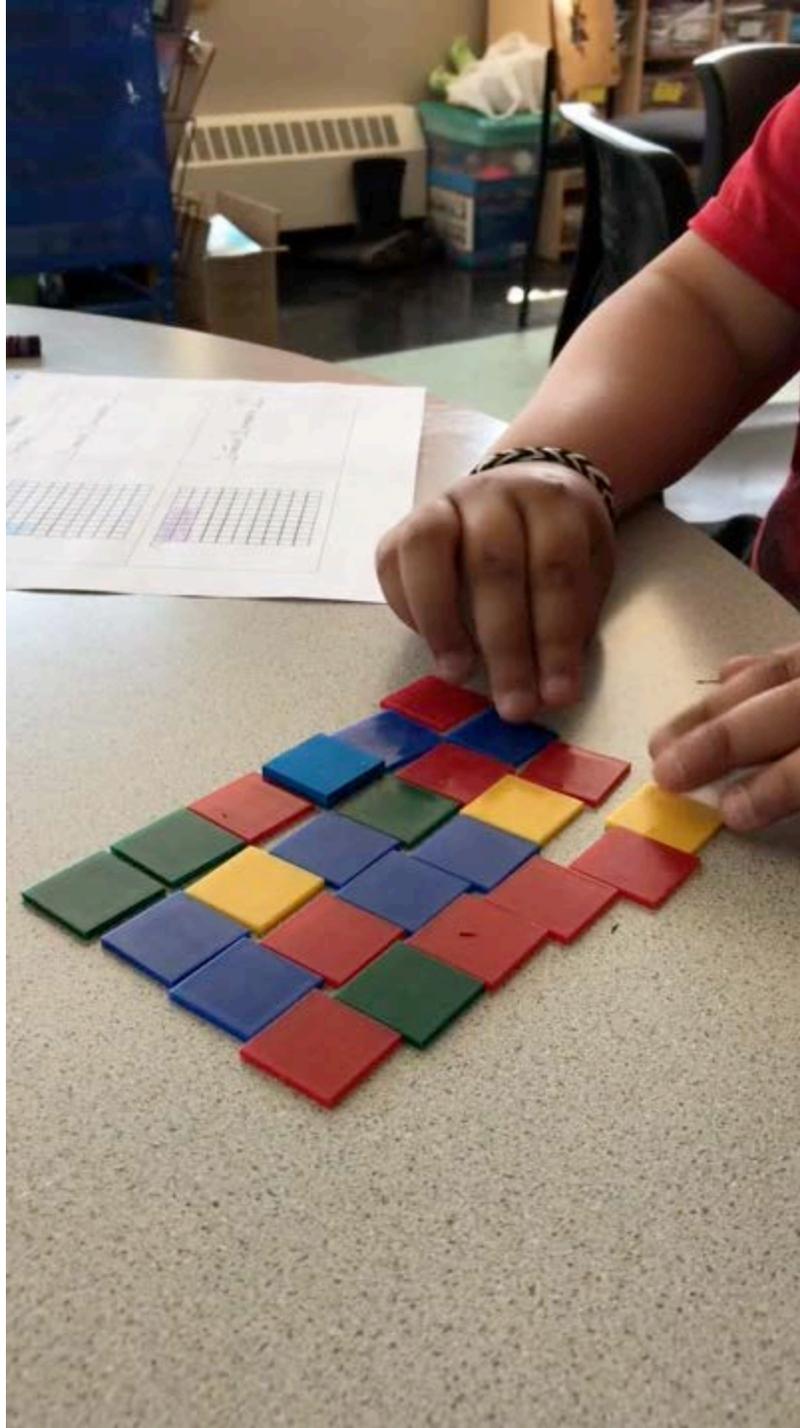
Shade 3 rows of 6.

Roll two dice to find the numbers for the blanks.



Record your results on the recording sheet.

3 rows of 6 is 18.



<https://photos.app.goo.gl/4gRnSeNBhzeZW8vw5>





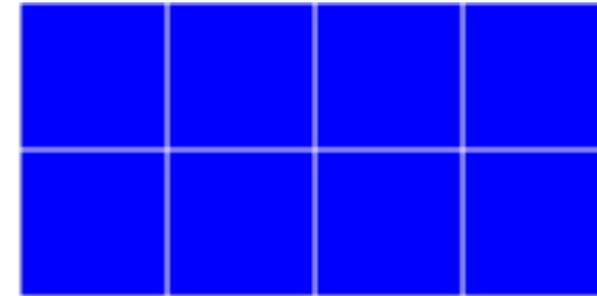
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# Findings from this series of tasks

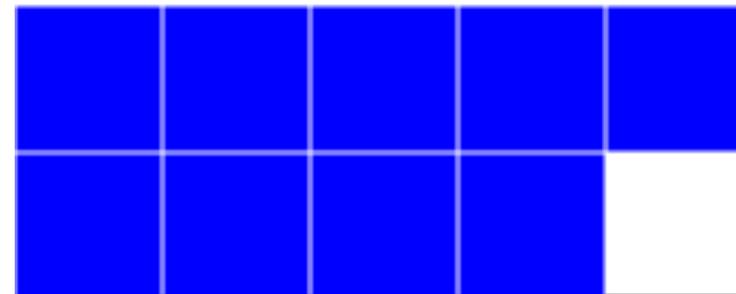
- Using the “of” language with actions of building allowed students to engage with the tasks and allowed us to see strategies for working with multiplication concepts;
- Transferred building approach from sets of to story problems;
- Coming to know in their own ways, using their own descriptions
  - “I built it 4 times, I built this 3 times...wait, this is just times...You guys! This is just times!”
- When we figure it out we name it!
- Teacher designed similar tasks for introducing multiplication
- Centres allow for exposure to various strategies; Story problems allow for selection of preferred or efficient strategies & appropriate models to fit the story context

# Can you organize it in two equal rows?

14	24	19
25	17	28
18	21	32



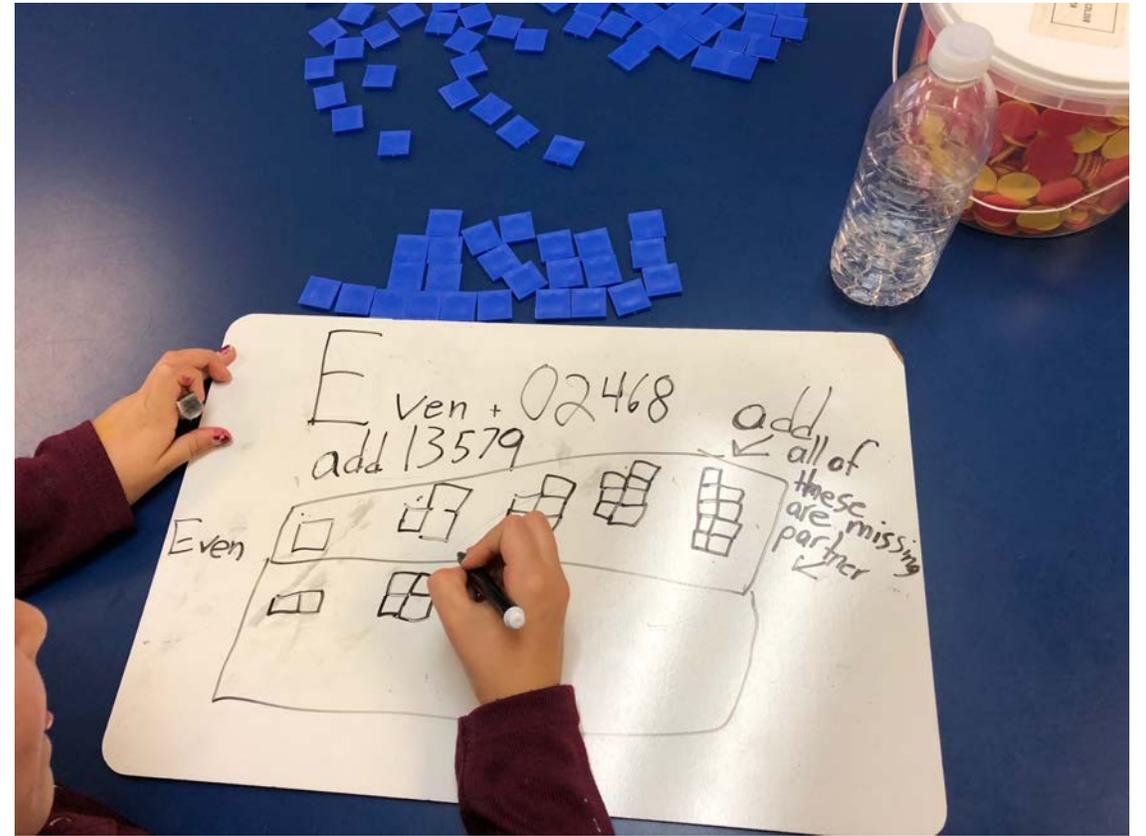
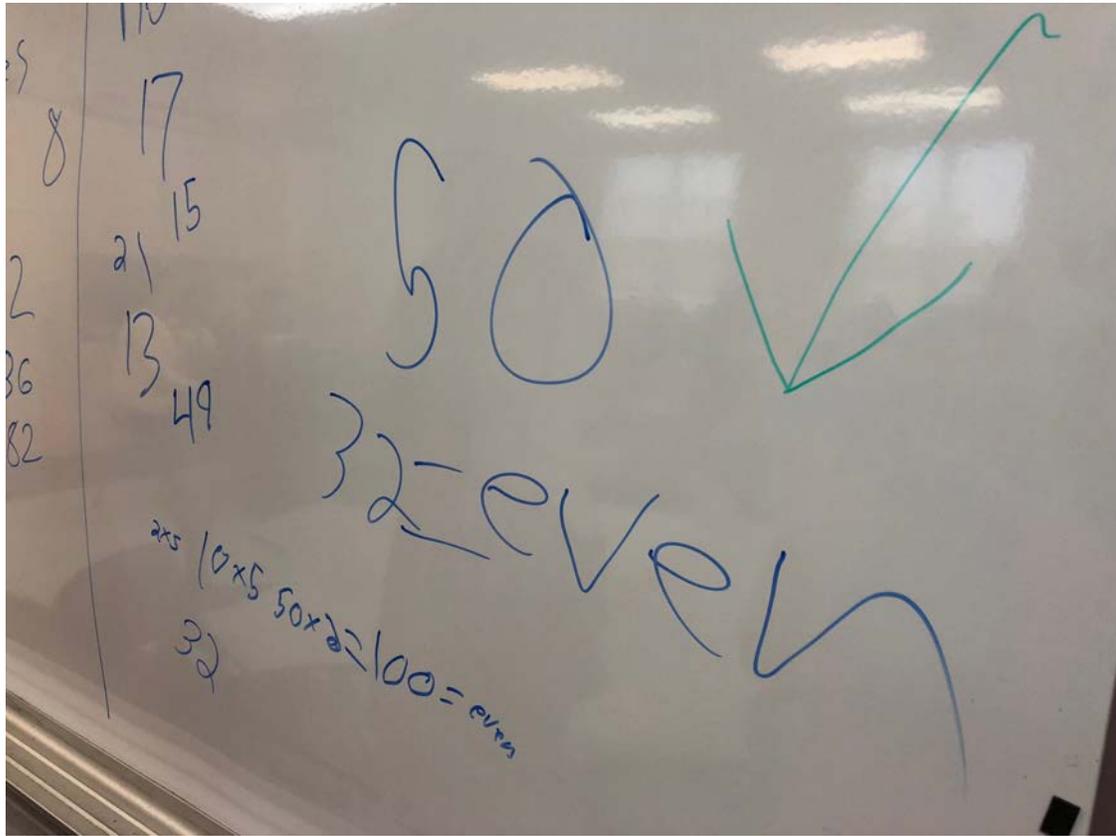
8 - Yes



9 - No

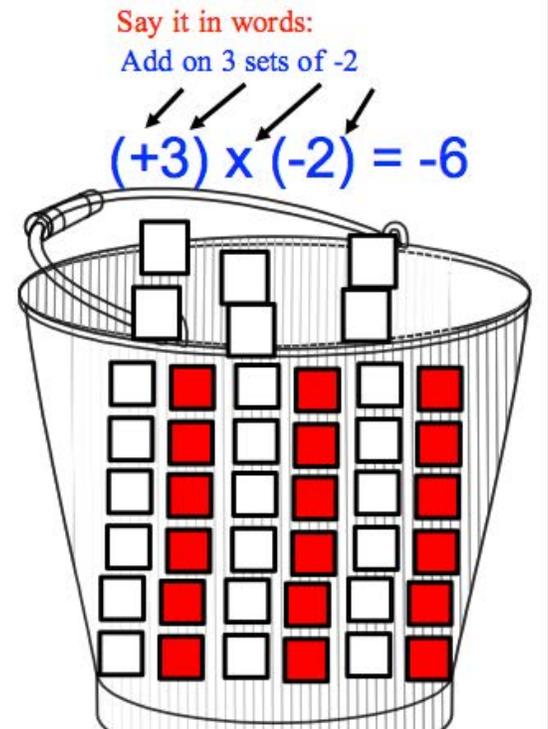
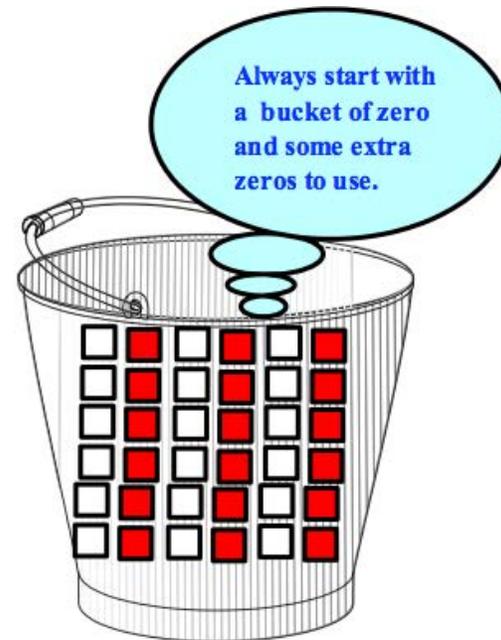
# Proof and Conjecture

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# Multiplying Integers

- The Bucket of Zero
- Adding to or taking from zero



# The bucket of zero

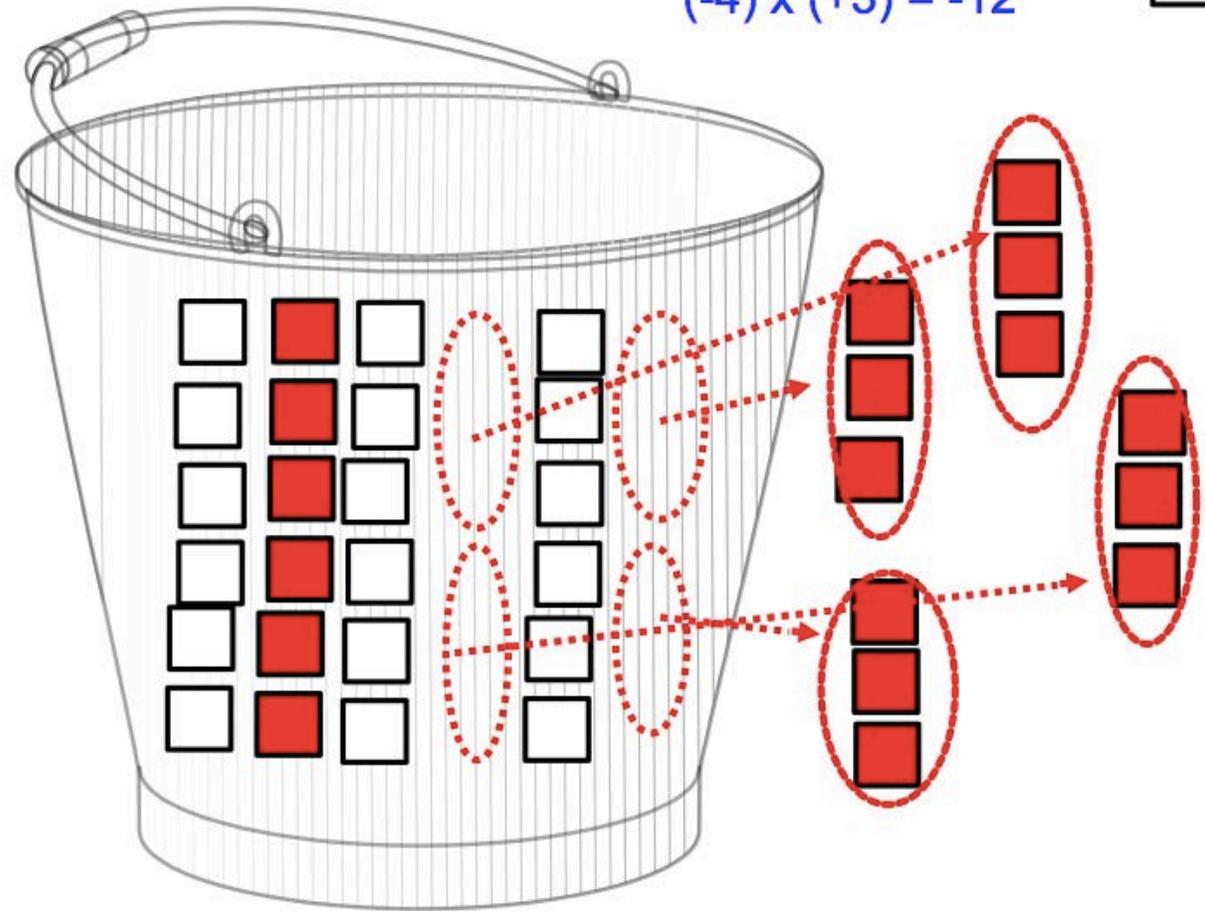
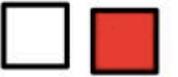
Taking away positives, leaves the bucket negative

Say it in words:

Take off 4 sets of +3

$$(-4) \times (+3)$$

$$(-4) \times (+3) = -12$$

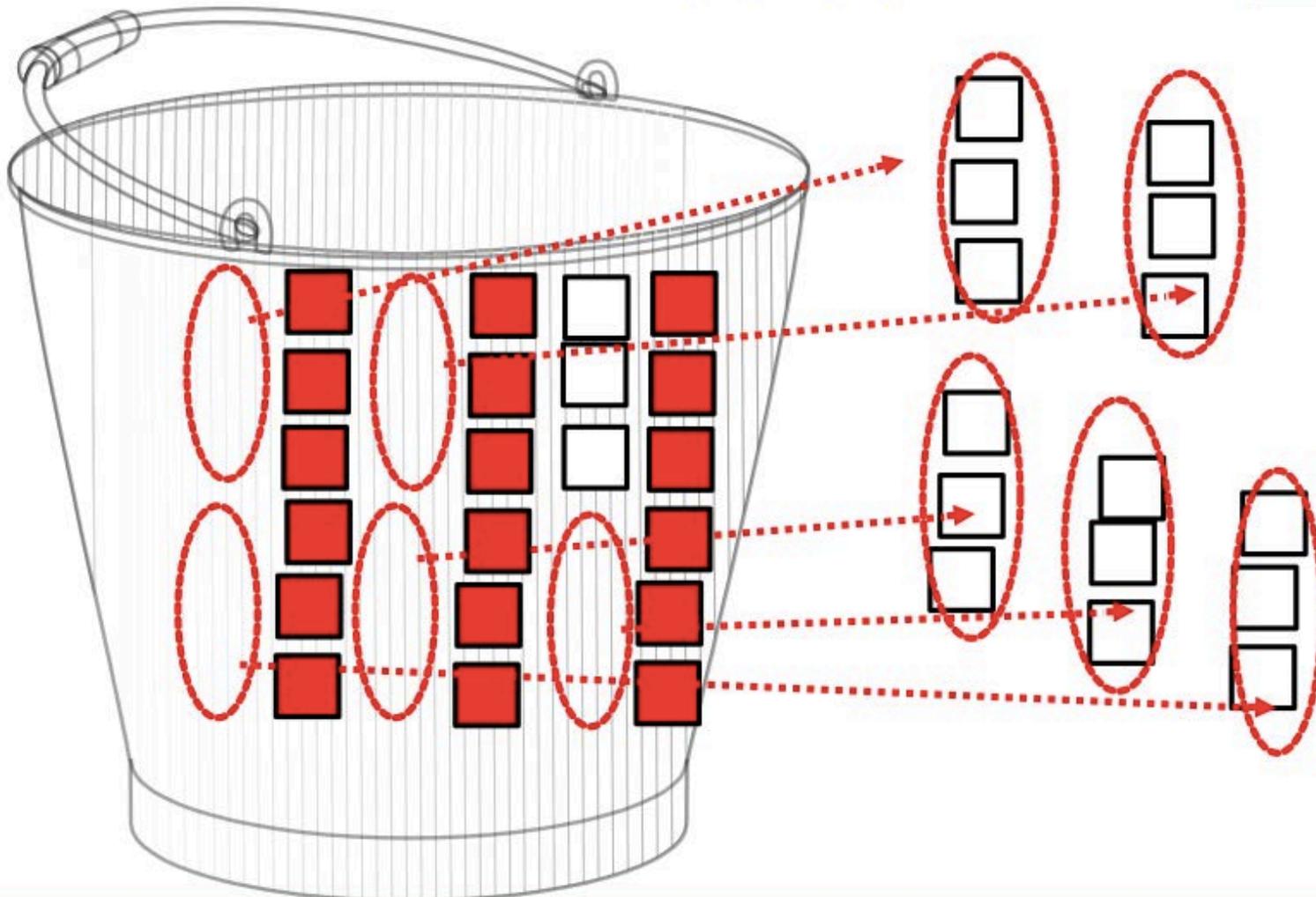
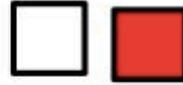


Say it in words:

Take off 5 sets of -3

$$(-5) \times (-3)$$

$$(-5) \times (-3) = +15$$



The bucket  
of Zero

Taking away negatives,  
leaves the bucket positive

# Current work: Holistic Math Assessments

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## Aliet Discovers Her Numbers





Whole	
 Part	 Part



Whole



Part



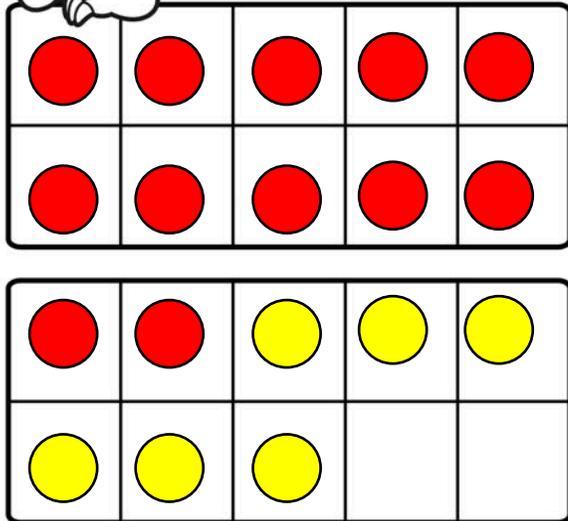
Part

# Making sets with 2 colours

I built 18 on my ten frame. I used 12 red and 6 yellow. What can you build?



Ten Frames with Aliet

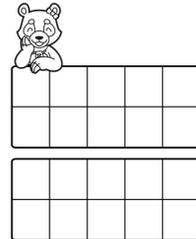


Roll for a number!

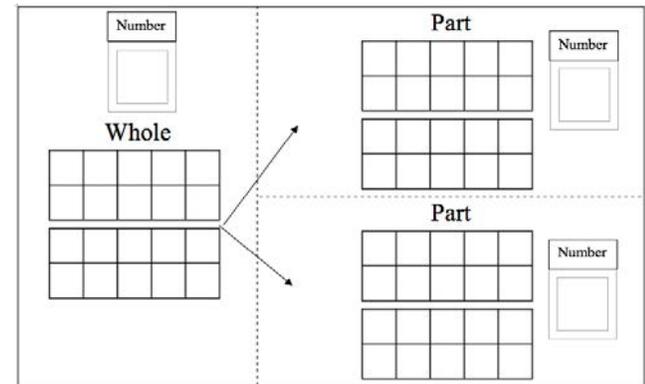


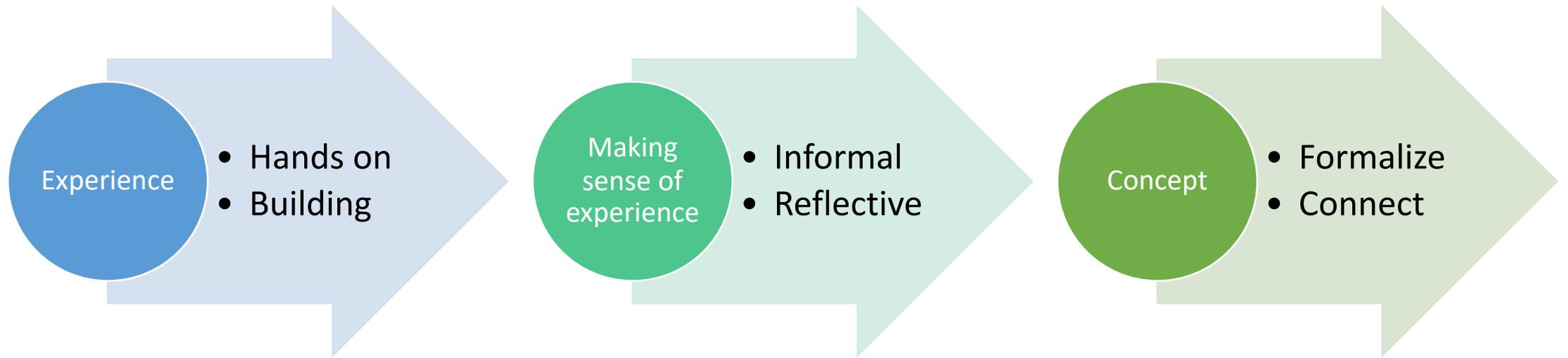
Build it on the ten frame using yellow and red!

Ten Frames with Aliet



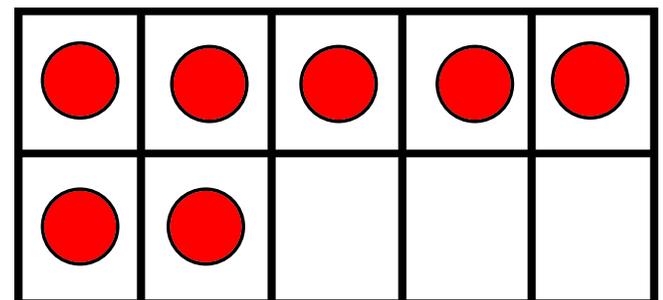
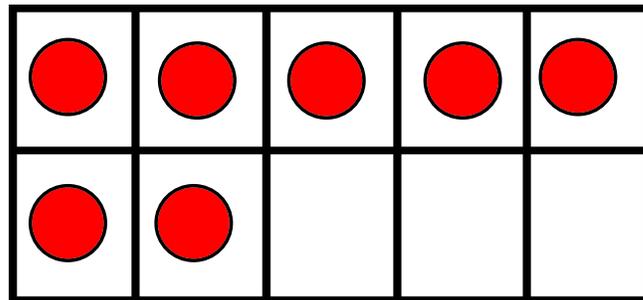
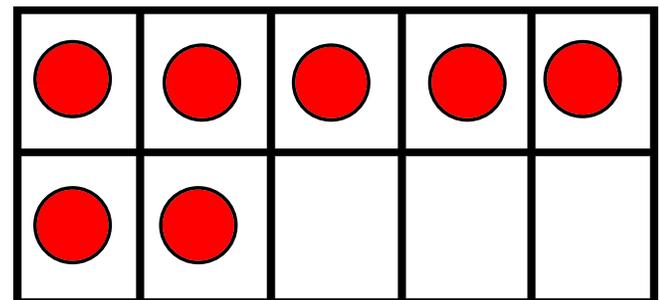
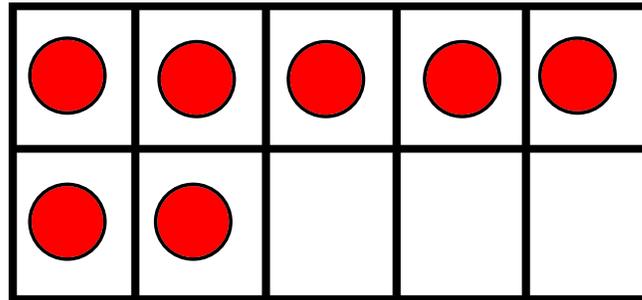
Record what you built!



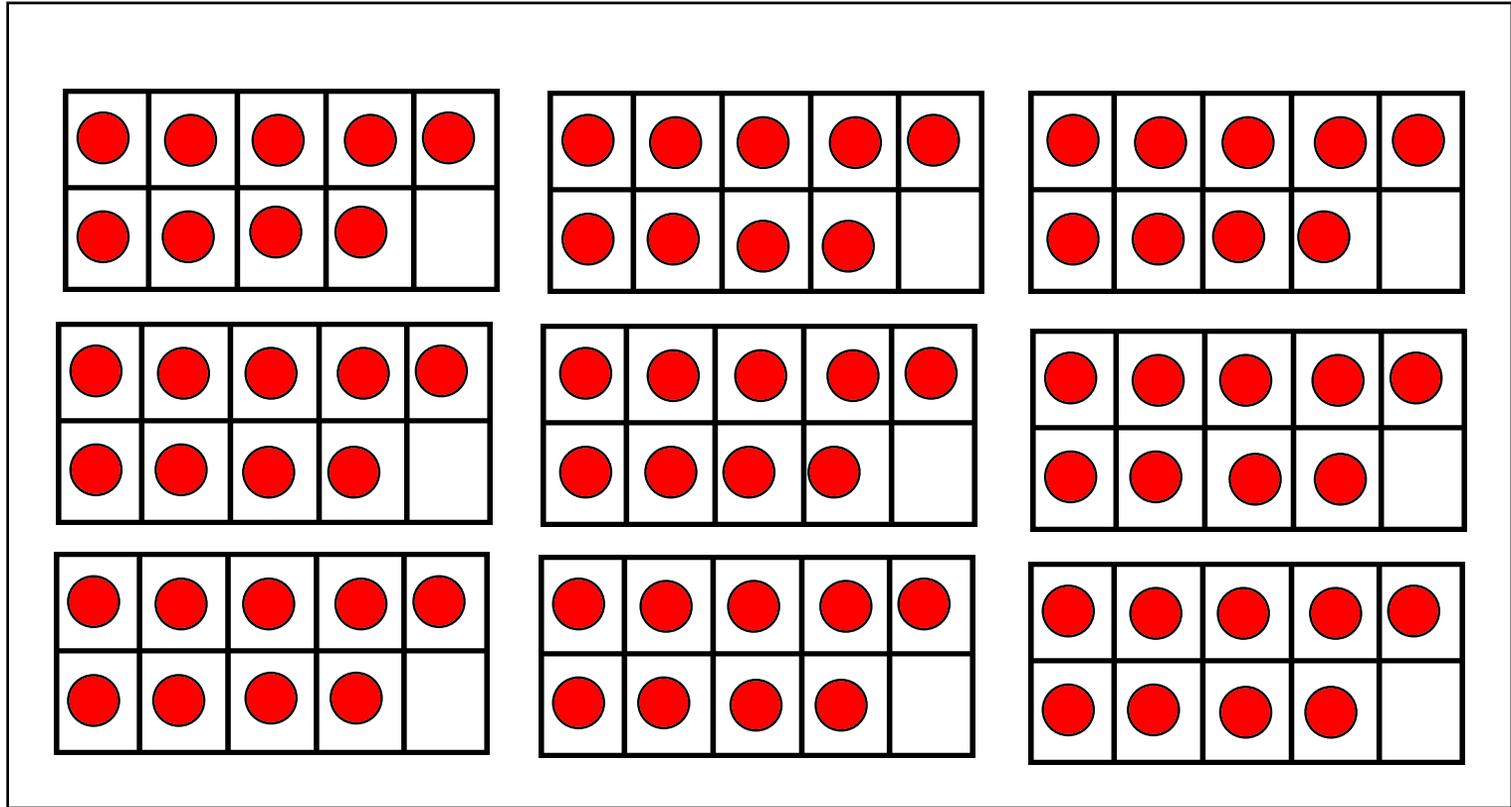


When we figure it out, we name it...

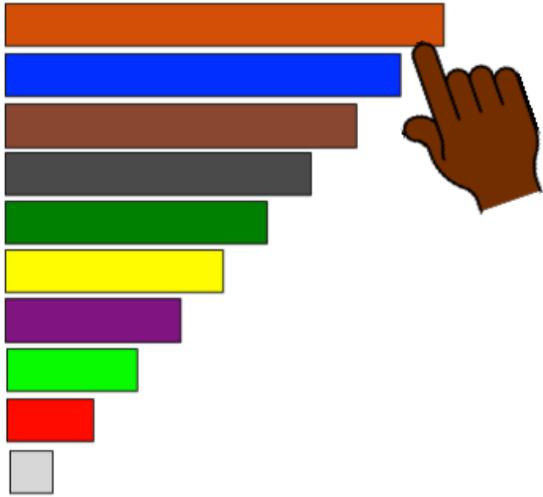
HOW CAN  
THIS HELP  
US WITH  
OUR 7S  
FACTS?



NOW LET'S  
EXPLORE  
OUR 9S  
FACTS!



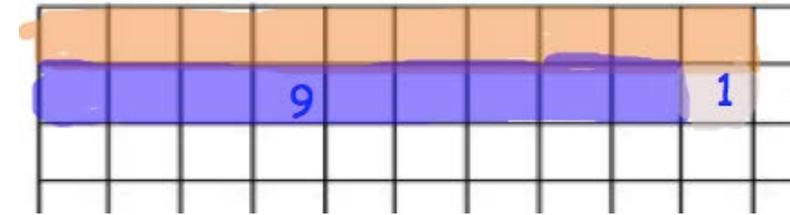
Choose the orange rod.



Find two rods that make the same length as the orange rod.



Record on grid paper.

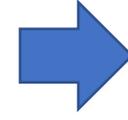


Making Trains – Partners for Orange

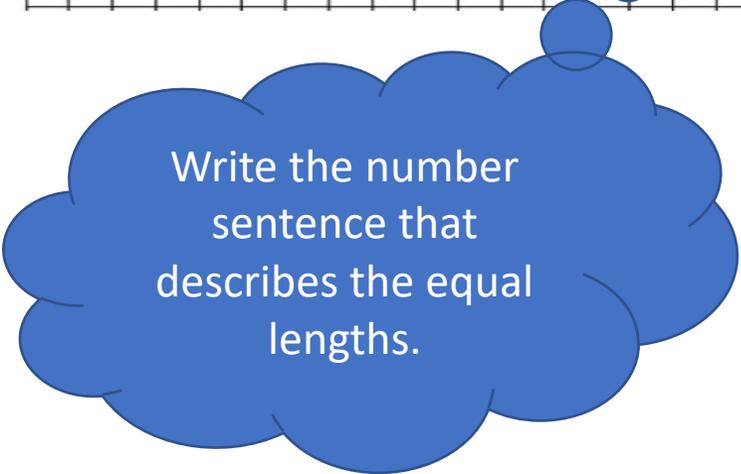
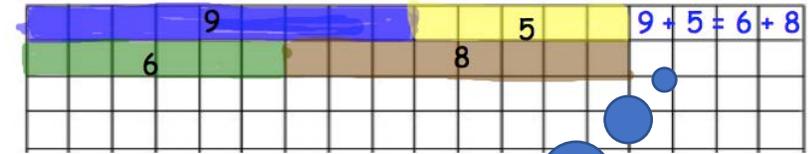
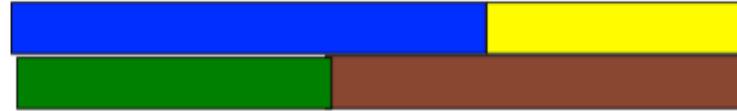
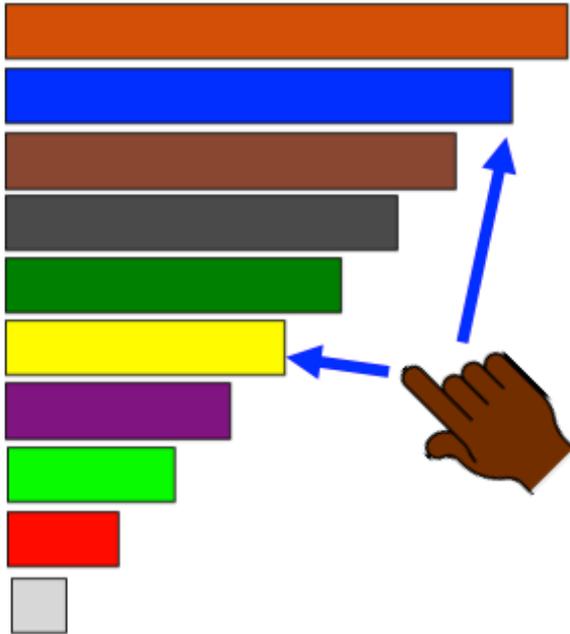
Choose two rods.



Find two different rods that make the same length.



Record on grid paper.

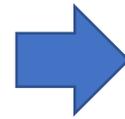


# Making Trains – Two Rods

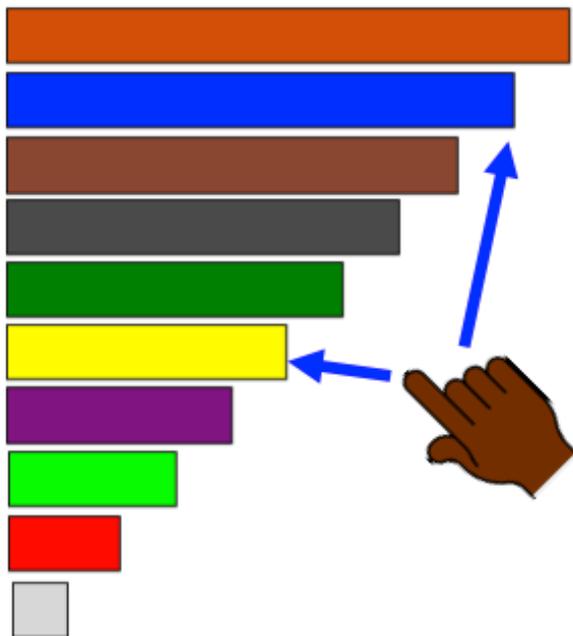
Choose two rods



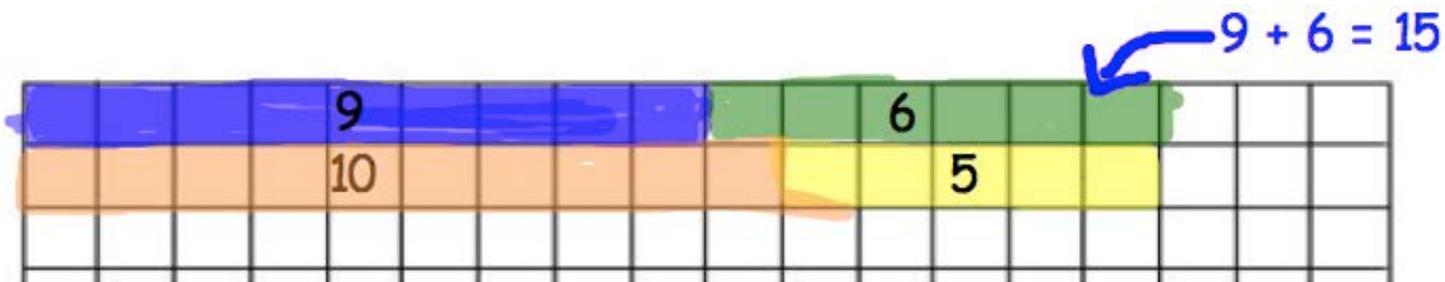
Combine them to make a long train.



Use the orange to find the total length.

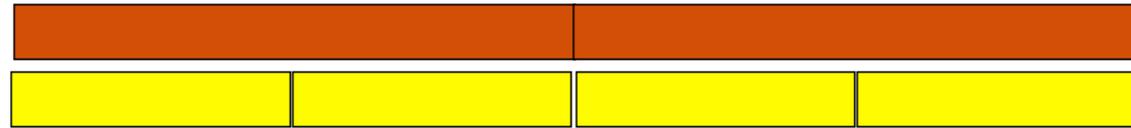


Record on grid paper.



# Making Trains – Helpful Orange

Multiplying  
and Dividing



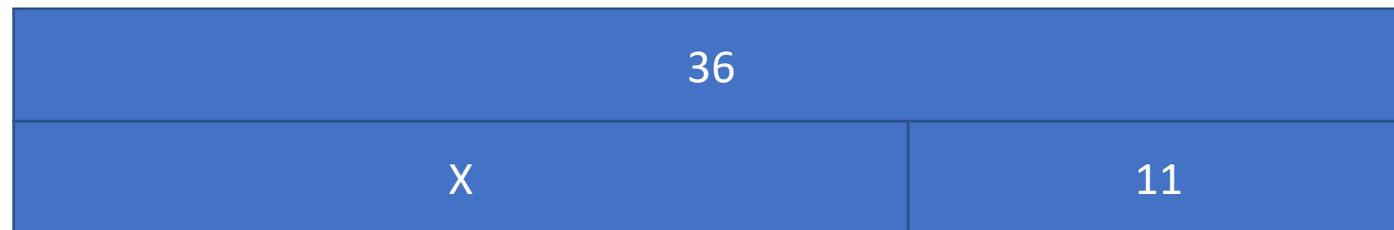
$$4 \times 5 = 2 \times 10 = 20$$

$$19 \div 6 = 3 \text{ R } 1$$



From rods to  
strip  
diagrams

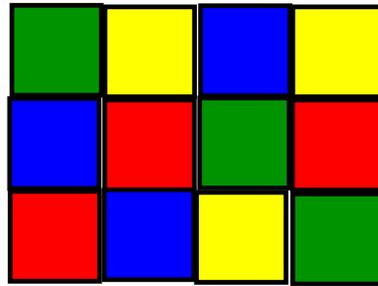
$$X + 11 = 36$$



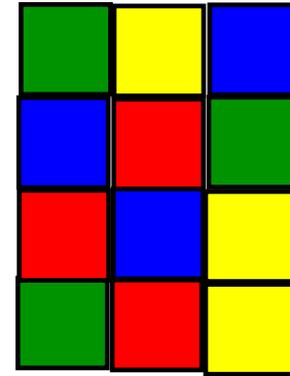
$$3x - 5 = 22$$



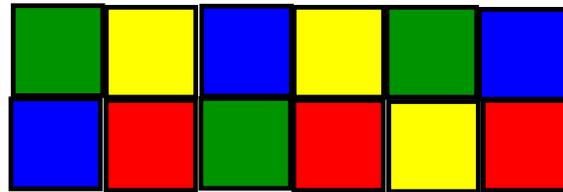
# Arrays and Areas



$$3 \times 4 = 12$$

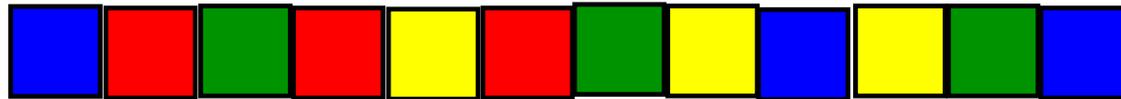


$$4 \times 3 = 12$$



$$2 \times 6 = 12$$

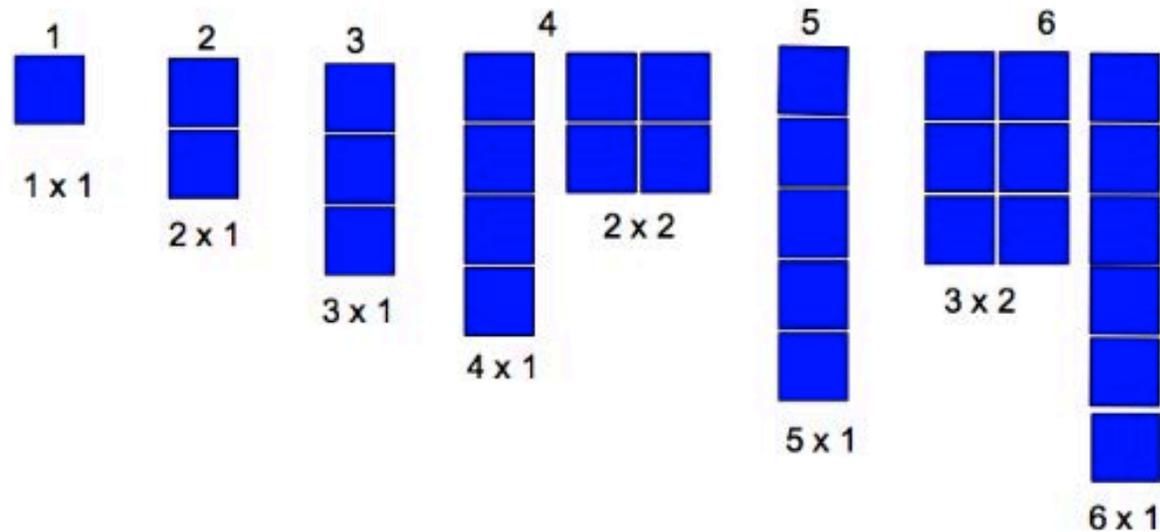
$$1 \times 12 = 12$$



## The Shape of a Number

Use square colour tiles to make rectangles with areas from 1 to 20.  
Record the dimensions of these rectangles on grid paper and complete a chart similar to the one below.

Note: When we talk about whether it make a rectangle in more than one way we will consider any rotation of a rectangle to be the same rectangle (i.e. a 2 by 1 and 1 by 2 will be considered as only one rectangle so 2 can be made in only one way).



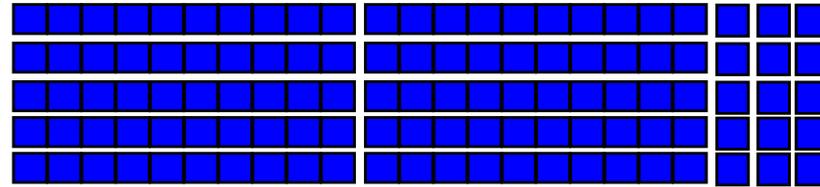
Number	Makes a rectangle		Makes a square	
	Only one way	More than one way	Yes	No
1	X		X	
2	X			X
3	X			X
4		X	X	
5	X			X
6		X		X
7				

# Explore...

- Look for patterns in the table. Do you notice anything about the numbers that can make a rectangle in only one way? Explain anything you notice about these numbers.
- Can you find numbers between 20 and 100 that can be made in only one way as well? What are they? How can you be sure their rectangles can be made in only one way?
- Look for patterns in the table. Do you notice anything about the numbers that can make a square? Explain anything you notice about these numbers.
- Can you find numbers between 20 and 100 that can a square as well? What are they? How can you be sure you have found all the square numbers up to 100? Explain.



# Multi-Digit Calculations with Area



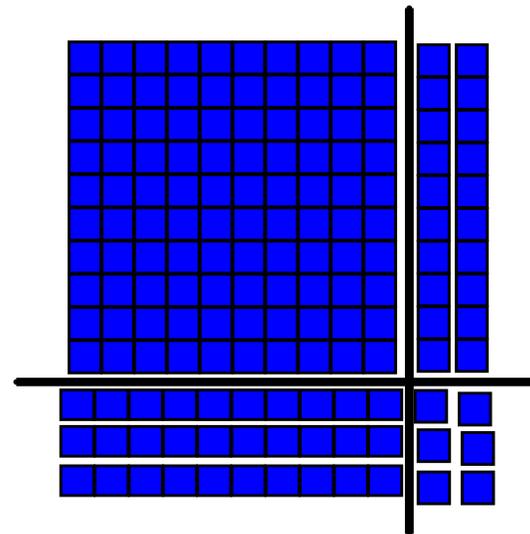
5 rows of 23

$$5 \times 10 = 50$$

$$5 \times 10 = 50$$

$$5 \times 3 = 15$$

$$5 \times 23 = 115$$



13 rows of 12

$$10 \times 10 = 100$$

$$3 \times 10 = 30$$

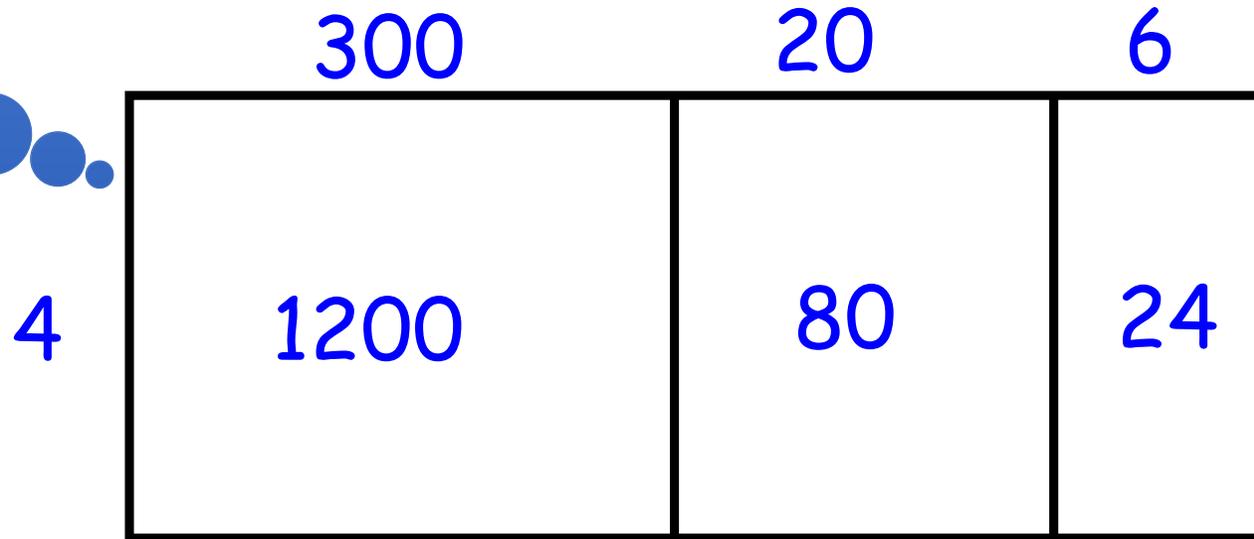
$$2 \times 10 = 20$$

$$2 \times 3 = 6$$

$$13 \times 12 = 156$$

# Area models

The area model can become a regional model to do 1 digit by 3 digit

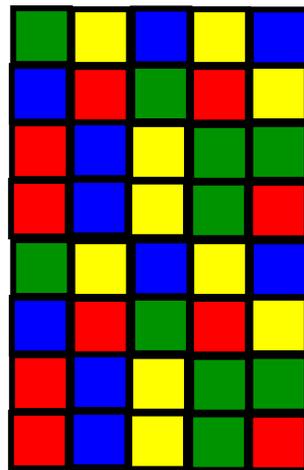


$$4 \times 326 = 1200 + 80 + 24 = 1304$$

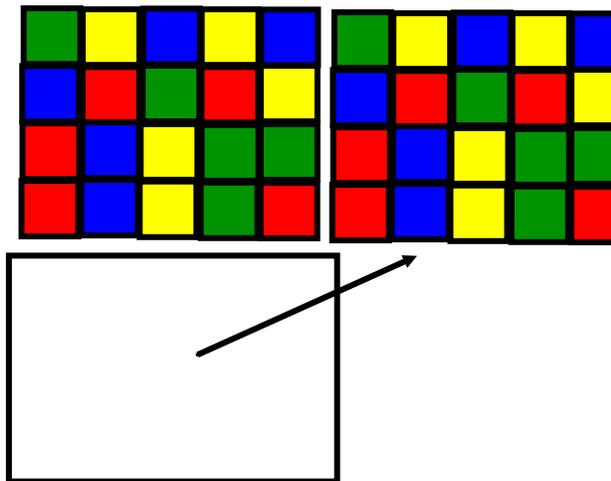
Halving and Doubling:  
The  
Associative  
Property

Show  $8 \times 5 = 4 \times 10$

$8 \times 5 = 4 \times 2 \times 5 = 4 \times 10$

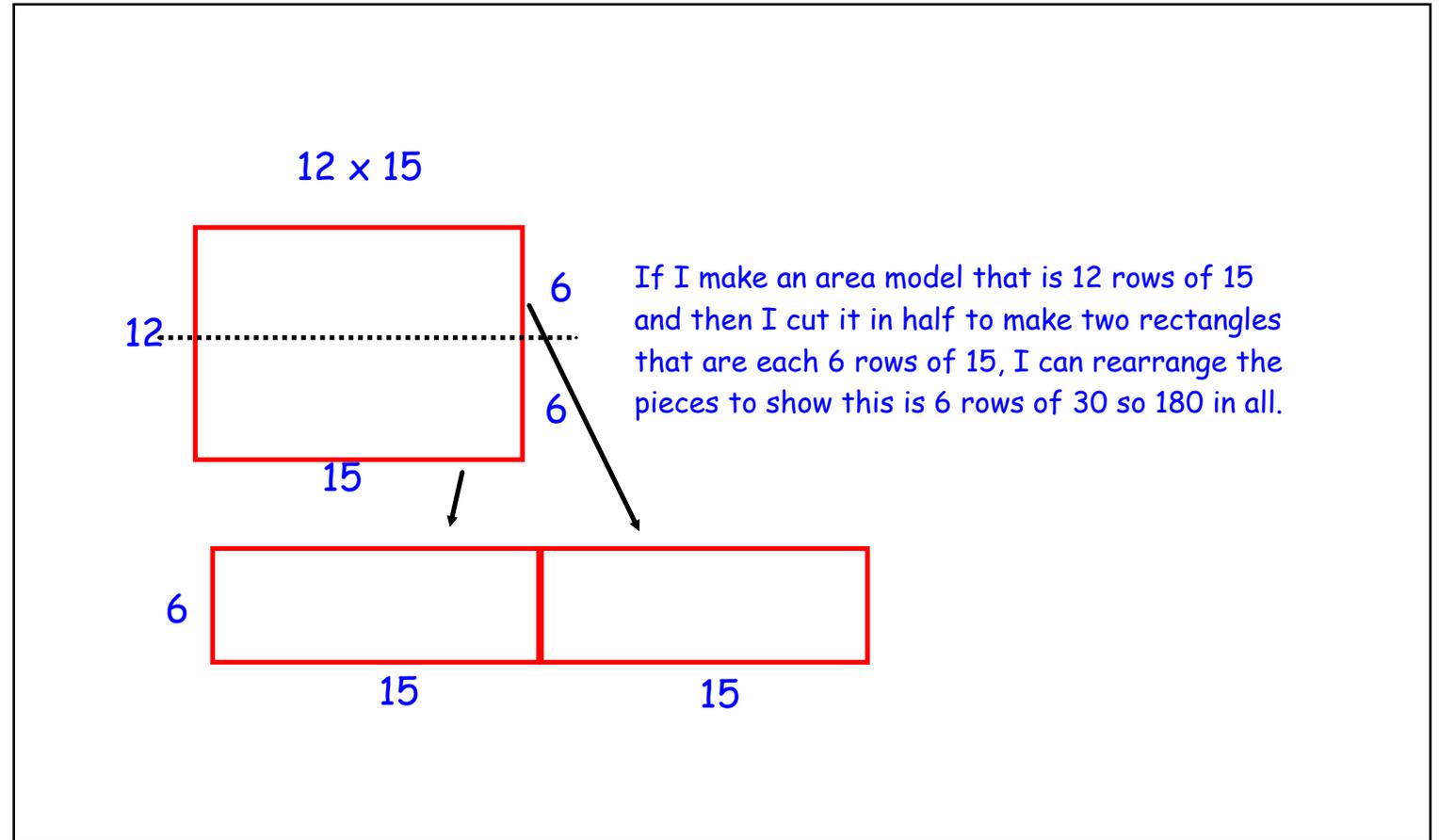


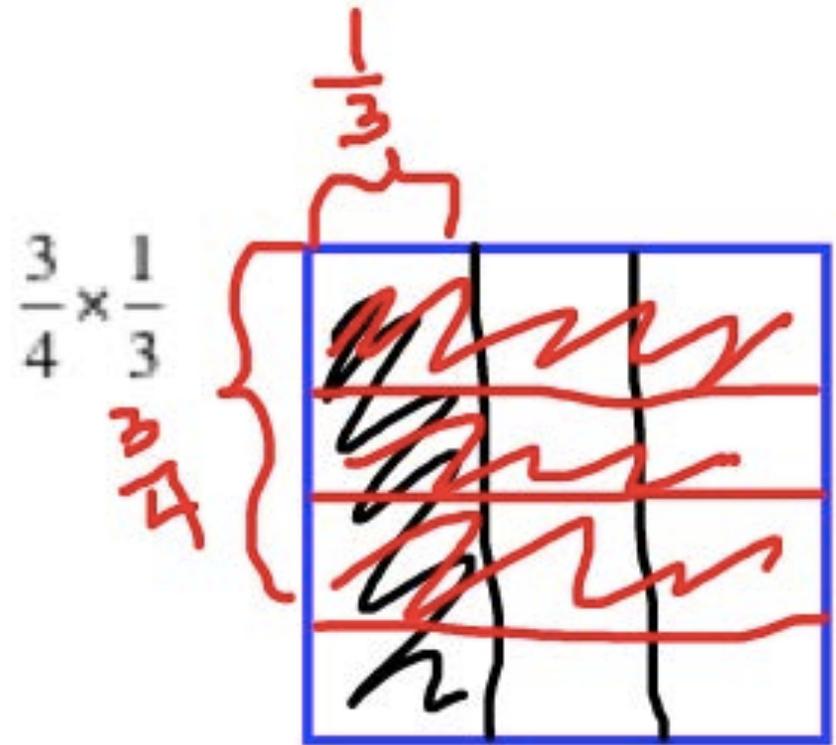
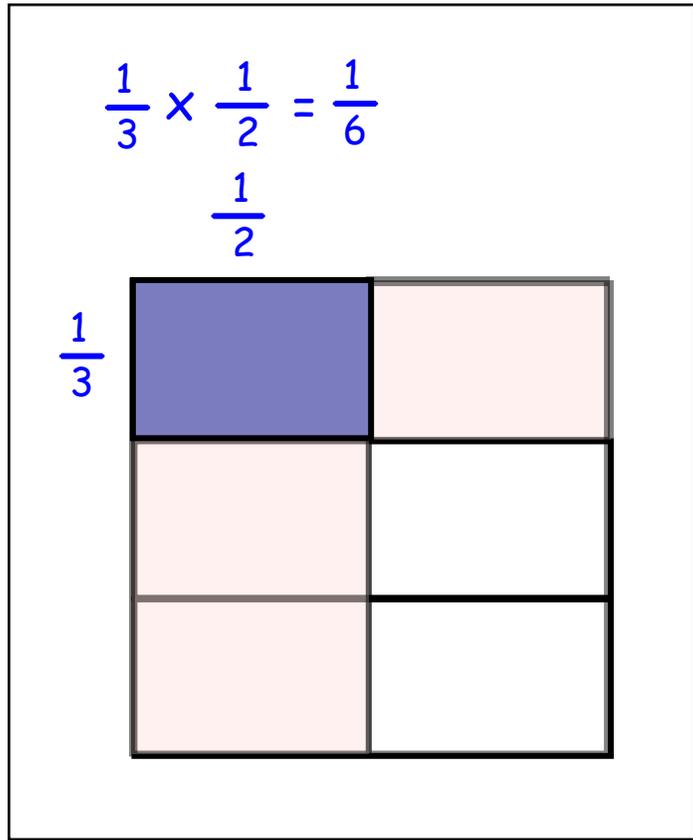
When I build 8 rows of 5 squares,  
I need 40 squares in all.



If I take off the 4 bottom rows  
and move them beside the 4 top  
rows, now I have 4 rows of 10,  
but it is still 40 squares in all.

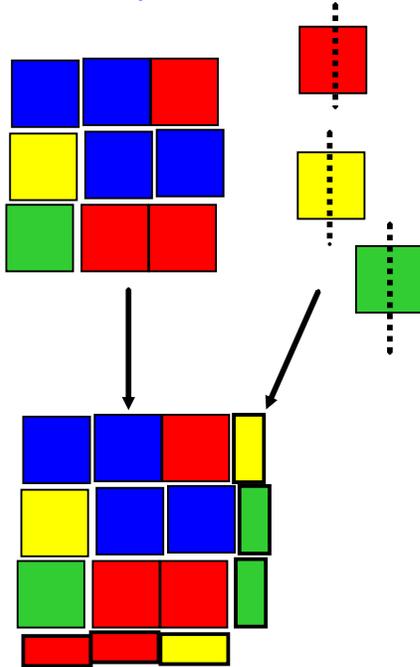
# Halving & Doubling





Multiplying Fractions with area...

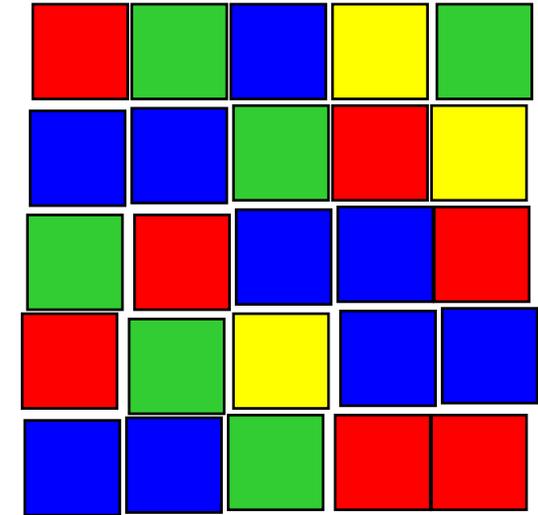
$$\sqrt{12} \approx 3.5$$



$$\sqrt{25} = 5$$

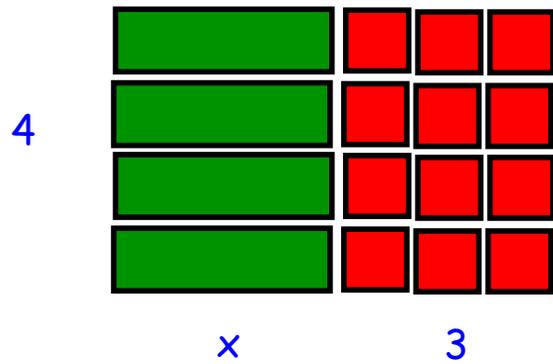
5

5

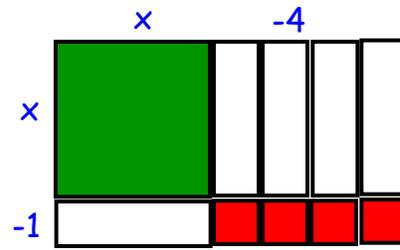


Square Root

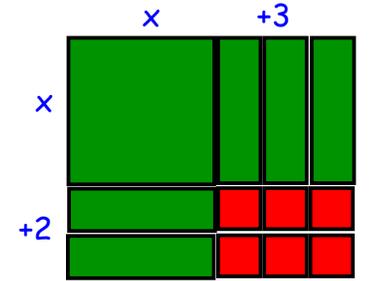
$$4(x + 3) = 4x + 12$$



$$(x - 1)(x - 4) = x^2 - 5x + 4$$



$$x^2 + 5x + 6 = (x + 2)(x + 3)$$



MODELING WITH ALGEBRA TILES

# Algebra





# Questions?

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Showmeyourmath.ca